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A COMPARISON OF BUFFER STRIP AND NON-BUFFER STRIP JOINT DESIGNS

James Michael Gill

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NAVAL POSTGRADUATE SCHOOL Monterey, California



THESIS

A COMPARISON OF BUFFER STRIP AND NON-BUFFER

STRIP JOINT DESIGNS

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James Michael Gill

June 1976

Thesis Advisor:

M.H. Bank II

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Buffer strip and non-buffer strip bolted wing skin type joints made from NARMCO 5208/T300 graphite-epoxy material were designed, and the excess bearing capacity and weight of these joints were calculated for a wide range of laminate compositions, bolt hole sizes, and number of bolt holes. Design load conditions representative of an advanced fighter type aircraft were chosen. Joint designs were arbitrarily restrained by assumed manufacturing con-

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A COMPARISON OF BUFFER STRIP AND NON-BUFFER STRIP JOINT DESIGNS

bу

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ABSTRACT

Buffer strip and non-buffer strip bolted wing skin type joints made from NARMCO 5208/T300 graphite-epoxy material were designed, and the excess bearing capacity and weight of these joints were calculated for a wide range of laminate compositions, bolt hole sizes, and number of bolt holes. Design load conditions representative of an advanced fighter type aircraft were chosen. Joint designs were arbitrarily restrained by assumed manufacturing conditions, assumed interface conditions, and imposed laminate composition restrictions. Charts were prepared from which relative joint efficiencies could be determined but no attempt was made to analyze the effect of the arbitrary design restrictions. The advantages and penalties for buffer strip design were discussed and recommendations for future studies were made.

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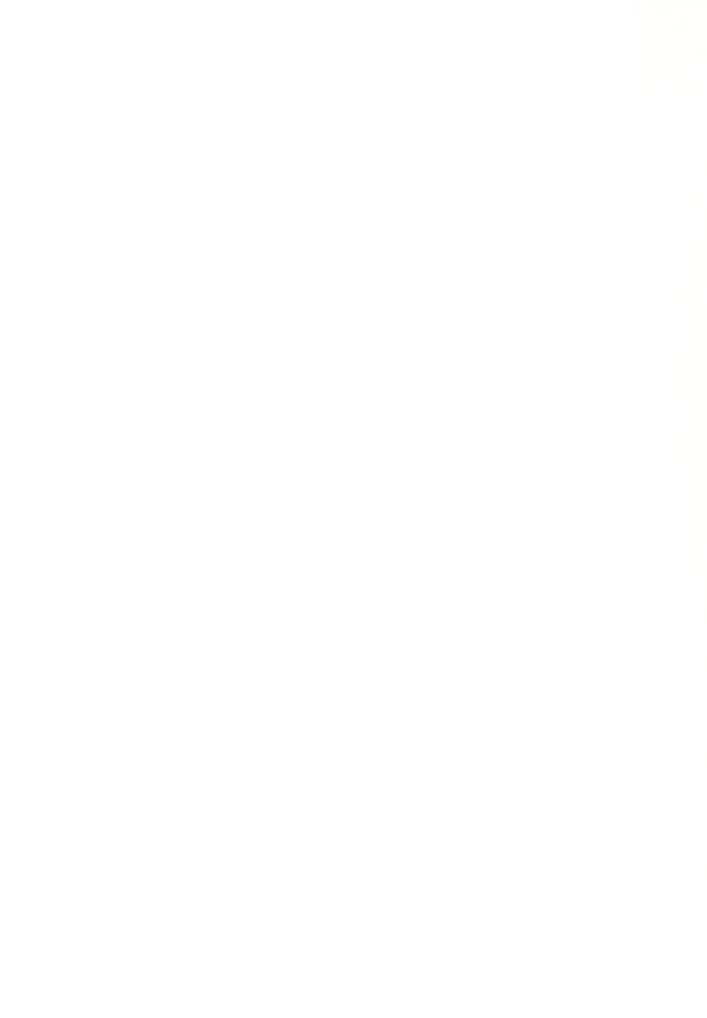
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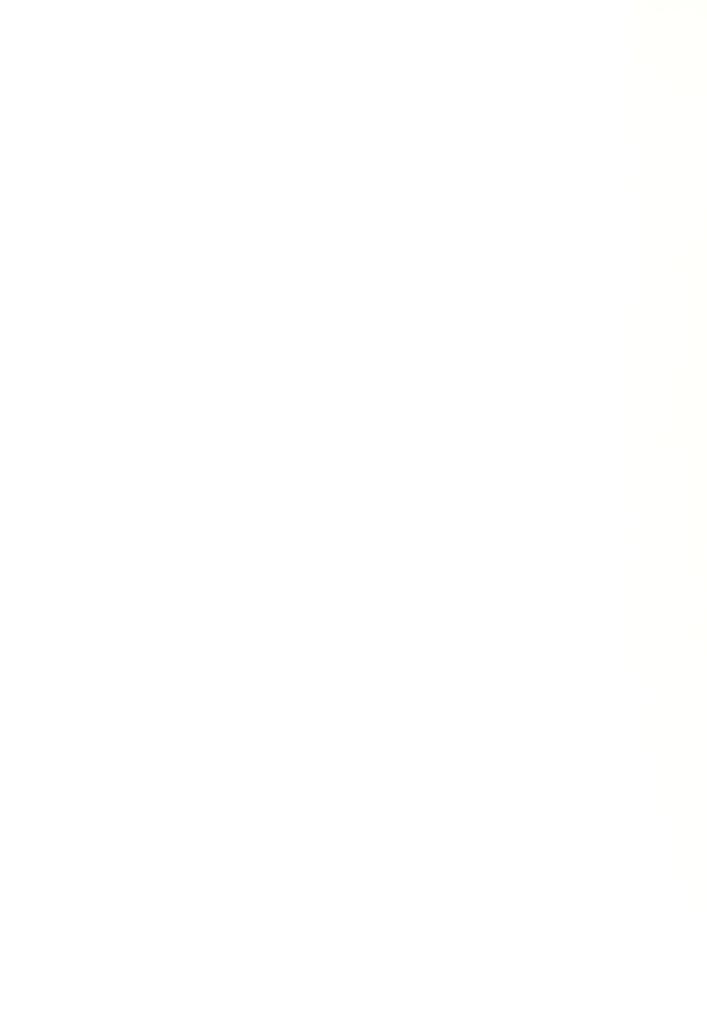
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LIST OF SYMBOLS

- AD = overall buffer strip joint width (in.)
- A_n = constant of proportionality between the bolt load P and the portion of P reacted each of the primary strips of a buffer strip joint
 - B = excess bearing capacity
 - D = bolt hole diameter (in.)
- E_{x} = tensile modulus (lbf./in.²)
- E_{x2} = tensile modulus of the buffer strip material in a
 buffer strip joint (lbf./in.²)
- F_{RP} = bypass force (lbf.)
 - F_S = shear load passing P_1 from a buffer strip to a primary strip (lbf.)
 - $F_r = reaction force (lbf.)$
- $f(\frac{a}{r})_{Q}^{i}$ = effective isotropic stress concentration factor at location i for load condition Q
 - f_s = shear stress between the buffer and primary strips
 of a buffer strip joint (lbf./in.²)
 - i = indicator of exact position on the hole
 - L = tensile load (lbf.)
 - L D = side length (in.)
 - M = number of rows of bolts in a buffer strip joint
 - m = reaction moment (in.-lbf.)
 - N = number of rows of bolts in a non-buffer strip joint
 - N_{x} = tensile load (lbf./in.)

```
N_{xv} = shear load (lbf./in.)
  P = tensile bolt load (lbf.)
 P = shear bolt load (lbf.)
 P_1 = portion of P reacted in each of the primary strips
       of a buffer strip joint (lbf.)
 P_2 = portion of P reacted in the buffer strip material of
       a buffer strip joint (lbf.)
  R = resultant bolt load (lbf.)
 S_1 = representative applied stress (lbf./in.<sup>2</sup>)
 S_2 = representative failure stress (lbf./in.<sup>2</sup>)
  t = plate thickness (in.)
  t* = effective plate thickness (in.)
t_{+4/5} = total thickness of \pm 4/5^{\circ} laminae (in.)
W_{\rm R}D = width of buffer strip material (in.)
W_1D = half-width of primary laminate material in a buffer
       strip joint (in.)
   Z = percentage of zero degree plies in the primary
       strips of a buffer strip joint
  \alpha = subscript denoting applied load conditions as
       follows:
       = bx bearing in x direction
       = by bearing in y direction
       = tx tension in x direction
       = ty
             tension in y direction
       = xy shear
  \epsilon = strain (in./in.)
 \lambda_{\alpha}^{1} = finite width correction factor at location i for
```

applied load condition α

 η = indicator of position in a joint

 $\sigma_{\rm BR}$ = resultant bolt bearing stress (lbf./in.²)

 σ^{i} = net tangential stress at location i

 σ_{α} = applied stress for load condition α

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I. INTRODUCTION

A. BACKGROUND

Aerospace structural design requirements have often been characterized by a demand for high strength and low weight. In many cases, the design possibilities have been limited by the available manufacturing technology and the acceptable manufacturing costs. The most successful designs were usually those which met all these constraints most efficiently.

The demand for high structural efficiency led to the development of advanced laminated composites which have higher strength-to-weight ratios and better fatigue properties than conventional structural materials (Ref. 1). As discussed in Ref. 2, it has also been possible to build laminated composite materials with higher modulus values than those characteristic of conventional materials. Accurate methods for tailoring the properties of such materials have evolved and such tailoring has become accepted design practice (Refs. 3,4,5). Waddoups, in Ref. 6, explained that significant gains in structural efficiency have been demonstrated by doing no more than substituting such a tailored composite for a conventional material keeping the geometry and mating interfaces the same.

These gains were realized because the composite materials used were less dense than the conventional

structural materials which they replaced. These material substitutions did not exploit the high strength and high modulus values achievable with advanced laminated composites.

B. OBJECTIVES

This study was intended to demonstrate the structural efficiencies which could be achieved by designs which took into account some of the high strength and high modulus properties of advanced composites. It was decided to demonstrate these efficiencies by analyzing the behavior of a plate of laminated material in the region of a bolted joint. This situation corresponded to that of a wing skin attached by a bolted fitting to the fuselage of an aircraft.

It was assumed that the wing skin would be attached to the aircraft fuselage through an aluminum alloy fitting. A maximum interbolt strain level, ϵ , of 3000 micro-inches per inch and an inter-bolt spacing of four hole diameters were taken as representative of such fittings.

Design conditions representative of an advanced fighter type aircraft were chosen. The joint was to carry a tensile load, $N_{\rm X}$, of 20,000 lbf. per inch of chord. It was assumed that the joint fittings would be covered by an aerodynamic fairing, and a maximum joint length of ten inches was allowed.

To keep the joint manufacture as simple as possible, it was decided that the skin thickness would vary linearly in the joint and that for any given joint design, all holes

would be of the same diameter. To simplify the analysis it was decided to limit the candidate materials to balanced design laminates composed of zero and ±45 degree plies of uniform thickness and material composition. No attempt was made to judge the effect of these restrictions on design efficiency.

The interface requirements determined by the aluminum fitting, and the geometric requirements to satisfy manufacturing simplicity, limited the possible joint designs and prevented full utilization of the high strength and high modulus properties available in the selected materials. It was felt, however, that even under these restrictions it would still be possible to demonstrate significant structural efficiencies by properly tailoring the laminates used in the wing skin.

C. RELIABILITY CONSIDERATIONS

Aerospace structural designs have had to meet difficult requirements for reliability. These designs have had to be sufficiently strong to carry the required loads and light enough to work in the aerospace environment. In addition to these requirements, critical components of aerospace structures have been expected to demonstrate that they are "fail-safe" and, in military applications at least, to some degree battle damage tolerant.

Early composite materials were judged inadequate for aerospace applications because they could not meet these reliability conditions. At first, quantity production of

advanced laminates was impossible because the required quality control technology did not exist. Wide batch-to-batch variation of the properties of these early materials justified only low confidence levels in their structural reliability. Although the early advanced composites were considered unreliable, materials research continued, driven by the anticipated structural efficiencies such materials could make possible. In 1973, Kaminski reported that NARMCO 5208/T300 graphite-epoxy laminates could meet the anticipated requirements for high strength, high modulus, and low weight and could be manufactured reliably and delivered with minimal batch-to-batch variation of material properties (Ref. 2). This was chosen as the structural material to be used in this study.

The requirement for battle damage tolerance and failsafe design is met by a variety of methods in designs with
conventional materials. These methods include built in
high excess load bearing capacity, alternate load paths,
and various crack stoppage stress relief devices. All of
these techniques can be applied to design with composite
materials. In addition to these techniques there is a
"buffer strip" material fabrication technique applicable to
laminated composites which provides an integral crack
stoppage capability. Kaminski and Eisenmann explained this
technique in Ref. 7.

In buffer strip design, integral "buffer strips" of low modulus, high fracture toughness material are included

in the laminate. These strips are spaced so that cracks originating in the high modulus load bearing primary strips are arrested when they run into the buffer strips. Using this technique, structures can be built in which cracks would be arrested before entire structural components failed. It appears that this could be an effective and efficient way to increase battle damage tolerance and the capability of a structural component to function after crack initiation.

D. RANGE OF THE STUDY

NARMCO 5208/T300 [0/±45] buffer strip and non-buffer strip joints were designed for widely varying laminate compositions, numbers and sizes of bolts. To simplify joint fabrication, the joint thickness was varied linearly between the inboard and outboard thicknesses, and all bolt holes for any given joint design were of the same diameter. To interface with the aluminum alloy fittings, the interbolt strain level was held to a maximum of 3000 micro-inches per inch, and the interbolt spacing was set at four hole diameters. The designs were compared to determine the effects of variation of hole size, number of holes, and laminate composition upon joint weight and excess bearing capacity.

Joint weight was considered a measure of the joint structural efficiency. Joint excess bearing capacity was considered a measure of allowable fabrication error. Since drilling holes in fibrous laminated composites has been

found to be both difficult and expensive, it was felt that the number of holes in any joint would be a measure of the relative joint fabrication cost (Ref. 5).

II. ANALYSIS OF THE NON-BUFFER STRIP JOINT

A. SIZING THE NON-BUFFER STRIP JOINT

Figure 1 is a schematic drawing showing the wing skin configuration used in the non-buffer strip joint design.

All bolt holes are of the same diameter. For this analysis, wing taper is disregarded and the bolt hole centers are assumed placed in parallel rows and columns four hole diameters apart.

In the following theoretical development, it is assumed that the applied tensile load, $N_{\rm X}$, and the applied shear load, $N_{\rm X}$, are constant across the outboard edge of the joint. Thus it is possible to size the joint considering only one column of bolts. It is further assumed that fittings were designed so that each bolt transfers the same portion, P, of the applied tensile load and that each bolt in the inboard row transfers, in addition to P, the same portion $P_{\rm S}$ of the shear load. In actual practice it is doubtful that this idealization could be achieved. However, it is a standard design assumption used in industry today (Ref. 3). This assumption implies a high resultant bolt load, R, in the inboard row of bolts.

From experimental analysis, it was known that layups of all ± 45 degree laminae would have a superior bolt load

bearing capacity (Ref. 9). Since the wing skin would be required to carry no applied load beyond the inboard row of bolts, it was decided to take advantage of this high bearing load capacity for all designs by requiring that, at the inboard row of bolts, the skin be composed of 100 per cent ±45 degree plies.

Considering a four-hole-diameters-wide column of bolts, the total tensile load L in the skin is given by

$$(1) \quad L = N_x 4D$$

where D is the bolt diameter used in the joint. If there are N bolts in each column,

(2)
$$P = \frac{L}{N} = \frac{N \times 4D}{N}$$

As explained in Ref. 10, the bearing stresses in a plate due to bolt loads are a function of the magnitude of the bolt load, the diameter of the bolt hole, and the effective thickness of the plate. For this study t*, the effective bolt bearing thickness of the plate, is defined as follows:

for
$$t \le 2D$$
, $t^* = t$

for
$$t > 2D$$
, $t^* = 2D$

where t is the plate thickness. This definition of effective bearing plate thickness is adopted to account for the fact that in thick plates loaded through a bolt hole the bolt loads tend to distribute themselves so that higher portions of the load are carried at the plate edges than at the plate center. The thickness definition was not chosen

through rigorous experimental or analytical processes but rather in light of engineering experience with metal plates. The bolt bearing stress, σ _{RR}, is

(3)
$$\sigma_{BR} = \frac{Bolt\ Load}{D\ t^*}$$

On all but the inboard row of bolts,

$$(4) \qquad \sigma_{\rm bx} = \frac{4 \, \rm N_{\rm x}}{\rm N \, t^*}$$

Since the inboard bolts in the non-buffer strip joints are assumed to react the shear as well as a share of the tensile load, they carry a bolt load, R, given by:

(5)
$$R^2 = \left(\frac{N_x + D}{N}\right)^2 + \left(N_{xy} + D\right)^2$$

(6)
$$R = 4DN_x \left[\left(\frac{1}{N} \right)^2 + \left(\frac{N_{XY}}{N_x} \right)^2 \right]^{\frac{1}{2}}$$

The bearing stress on these inboard bolts is

(7)
$$\sigma_{BR} = \frac{4N_X}{t^*} \left[\left(\frac{1}{N} \right)^2 + \left(\frac{N_{XY}}{N_X} \right)^2 \right]^{\frac{1}{2}}$$

Test specimens composed of NARMCO 5208/T300 $\left[\pm45\right]$ layers were found to be able to withstand

$$\sigma_{\rm BR}$$
max = 78000 lbf./in.²

when this load was applied through untorqued bolts (Ref. 9). This value is used in Eq. 7 to determine the minimum allowable joint thickness at the inboard bolt holes. In cases where this is a critical design parameter, the geometry illustrated in Fig. 2(a) is used to size the joint. Otherwise, the geometry illustrated in Fig. 2(b) is used.

The bolt hole center locations are numbered from one to N beginning with location 1 at the first or outboard bolt and ending with location N at the last or inboard bolt. To simplify the analysis, other locations in the joints are specified by a parameter η , defined relative to the bolt hole numbers. η = 1 means at the position of the first bolt hole center, η = 2 means at the position of the second bolt hole center, and η = N means at the position of the inboard bolt hole center. Intermediate positions are defined as follows:

 η = 1.5 means halfway between η = 1 and η = 2

 η = 2.5 means halfway between η = 2 and η = 3

 η = N-.5 means halfway between η = N-1 and η = N The bypass force, F_{BP}, in the joint is defined as the tensile load passed from station η to station η +1, thus,

$$F_{BP} = N_x 4D \left(1 - \frac{\eta}{N}\right)$$
 $(\eta = integer)$

The bypass stress, σ_{tx} , is defined as

$$\sigma_{\rm tx} = \frac{F_{\rm BP}}{4Dt}$$

The bypass strain ϵ is defined as

$$\epsilon = \frac{\sigma_{\text{tx}}}{E_{\text{x}}}$$

where $\mathbf{E_{X}}$ is the tensile modulus of the material. The strain level halfway between station η and $\eta\text{+}\mathbf{l}$ is given by

(8)
$$\epsilon_{\eta+.5} = \frac{N_{x} (1 - \frac{\eta}{N})}{t E_{x\eta+.5}}$$
 ($\eta = integer$)

Both thickness and tensile modulus of the material are allowed to change with location within the joint.

The stress-strain behavior of a zero degree NARMCO 5208/T300 lamina is linear to failure. As reported in Ref. 2, the modulus of elasticity of such a lamina in the direction of the graphite fibers was determined by experiment to be 20.5 X 10⁶ lbf./in.². The stress-strain behavior of a NARMCO 5203/T300 45 degree lamina is not linear. Tests performed in 1974, (Ref. 11), for a NARMCO 5203/T300 45 degree lamina under room temperature dry conditions reported the stress-strain behavior in the form of a secant modulus, which varied with strain level from 2.9 X 10⁶ lbf./in.² at zero strain to 1.3 X 10⁶ lbf./in.² at a strain level of 13000 micro-in./in. as shown in Fig. 3. (Secant modulus is the slope of a line through a point on the stress-strain curve and the origin.)

As explained in Ref. 3, the strain state for a balanced laminate composed of n layers is described by

where $\left[N\right]$ is a vector of applied tensile and shear loads and $\left[\epsilon\right]$ is a vector describing the strain state of the plate. The components of the $\left[A\right]$ matrix are defined as

follows:

(10)
$$A_{ij} = \sum_{k=1}^{n} \overline{C}_{ij}^{k} t_{k}$$

where \overline{C}_{ij} are the elements of the compliance matrix of the k^{th} lamina.

This study is concerned only with balanced design laminates made from laminae of uniform thickness and material composition and oriented at either zero or ±45 degrees to the spanwise direction. For such laminates, it is seen from Eqs. 9 and 10 that the various moduli vary linearly with the per cent of zero degree plies in the laminate. Because the ±45 degree data on secant modulus was available, and because the secant modulus is convenient for design use, a laminate value of secant modulus was calculated. Figure 4 shows the variation of secant modulus with laminate composition for NARMCO 5208/T300 $0/\pm45$ material at ϵ = 3000 micro-in./in. It was prepared assuming that this modulus varies linearly between the experimentally determined values for such laminates with zero and 100 per cent zero degree plies. Figure 4 is used to determine the tension modulus of the various NARMCO 5208/T300 $0/\pm45$ laminates used in the study joint designs.

The laminate composition at station $\eta=1.5$ is assumed to be the same as that of the wing skin outboard of the joint. It determines the tensile modulus at this position. Equation 8 is then used to determine $t_{1.5}$.

The laminate composition at station η = N-.5 is initially

determined by assuming that the percentage of zero degree plies varies linearly from station $\eta=1.5$ to station $\eta=N$ where the laminate is to be composed of 100 per cent ± 45 degree plies. An additional constraint, applicable only to the non-buffer strip joint, is that the laminate at station $\eta=N-.5$ can have no fewer than 5 per cent zero degree plies. This is done to ensure that there are sufficient load bearing zero degree plies to carry the bypass load between the second to last and the last, or inboard, row of bolts.

Having fixed the laminate composition, the tensile modulus and, through Eq. 8, the thickness at station N-.5 are determined.

The remaining joint thicknesses are determined assuming a linear variation of joint thickness between $\eta=1.5$ and $\eta=N-.5$. Laminate compositions midway between each pair of adjacent bolts are determined using the thickness distribution and the desired strain level.

(11)
$$E_{x\eta+.5} = \frac{N_x (1 - \frac{\eta}{N})}{t_{\eta+.5}}$$
 ($\eta = integer$)

The tension modulus, $\mathbf{E}_{\mathbf{X}}$, of the material is assumed to vary linearly with distance between the values determined from Eq. 11. Thus,

(12)
$$E_{x_{\eta}} = \frac{E_{x_{\eta-.5}} + E_{x_{\eta+.5}}}{2} \qquad (\eta = integer)$$

These modulus values determine the laminate composition throughout the joint.

Joints are sized using 0.25, 0.375, 0.4375, and 0.5 inch bolts with laminate compositions at the first bolt varying from 60 to 10 per cent zero degree plies. These laminate compositions cover the range over which the Eisenmann strength model to be described in the next section was considered accurate. In all cases, the same interbolt strain level, 3000 micro-inches per inch, is maintained. The minimum number of bolts used in any joint design is three. This is done to provide a mechanism by which the desired strain level can be maintained. The maximum number of bolts in any joint is determined by the desired interbolt spacing of four bolt hole diameters and the requirement that the joint length not exceed ten inches.

B. DETERMINING THE STRENGTH OF A NON-BUFFER STRIP JOINT Waddoups, Eisenmann, and Kaminski, in Ref. 12, showed experimentally that graphite-epoxy laminates are statically brittle and exhibit many of the failure characteristics of brittle materials first explained by Griffith in Ref. 13. They formulated a model which assumed that crack growth behavior in graphite-epoxy laminates was a function of stress intensity and critical energy level, and they verified their model by experiment.

In Ref. 14, Eisenmann continued this work and developed a bolted joint strength model for composite materials. This model accounted for the material ultimate strengths, local stress intensity factors, and geometric width correction factors. With the Eisenmann model, it was

possible to calculate the total stress at any point on a loaded circular hole in an orthotropic plate by linearly combining the various stresses acting upon the plate using Eq. 13. Because of the internal curve fitting techniques used in this model, it was considered to give accurate results for laminate compositions varying from 10 to 60 per cent zero degree plies (Ref. 14).

(13)
$$\sigma^{i} = \lambda^{i}_{tx} f(\frac{\underline{a}}{r})^{i}_{tx} \sigma_{tx} + \lambda^{i}_{ty} f(\frac{\underline{a}}{r})^{i}_{ty} \sigma_{ty}$$
$$+ \lambda^{i}_{xy} f(\frac{\underline{a}}{r})^{i}_{xy} \sigma_{xy} + \lambda^{i}_{bx} f(\frac{\underline{a}}{r})^{i}_{bx} \sigma_{bx}$$
$$+ \lambda^{i}_{by} f(\frac{\underline{a}}{r})^{i}_{by} \sigma_{by}$$

where:

i = indicator of the exact position on the hole.

 λ_{α}^{i} = finite width correction factor at location i for applied load condition α

 $f(\frac{a}{r})^{i}_{\alpha}$ = effective isotropic stress concentration factor at location i for applied load condition α

 σ_{α} = applied stress for load condition α

 σ^{i} = net tangential stress at location i

a = subscript denoting applied load condition as
follows:

xy = shear

tx = tension in x - direction

ty = tension in y - direction

bx = bearing in x - direction

by = bearing in y - direction

The stress definitions are sketched in Fig. 5. The λ and f factors are determined by plate geometry and material composition.

The failure modes of NARMCO 5208/T300 $\left[0/\pm45\right]$ plates with loaded holes were determined by test (Ref. 14). Crack initiation in the test specimens most often occurred on the hole edge at positions β =0, \pm 45, \pm 90, \pm 135, or 130 degrees measured from the X axis. From symmetry it was determined that all these failure modes could be adequately described by description of the failure modes encountered at β =0, 45, and 90 degrees. Laminate strength for each of these positions was determined by experiment (Ref. 14). In these tests the bolts used to load the holes were untorqued.

The Eisenmann static strength model was used to calculate stress intensity and geometric width correction factors based upon an interbolt spacing of four hole diameters. Equation 13 was used to prepare Figs. 6-29 which define the failure modes expected for laminates whose composition varies from 60 to 10 per cent zero degree plies with 0.25, 0.375, 0.4375, and 0.50 inch holes. Only the effects of $\sigma_{\rm XY}$, $\sigma_{\rm tx}$, and $\sigma_{\rm bx}$ were considered in the preparation of these curves.

One of the parameters of interest in this study is the excess bearing capacity of each joint design. For purposes of this study the excess bearing capacity of the joint is defined as the smallest excess bearing capacity at any

bolt hole in the joint. At each hole a representative stress load, S₁, which accounts for the combined bearing and bypass stresses is calculated as follows:

(14)
$$S_1 = \begin{bmatrix} \sigma^2 + \sigma^2 \\ bx + \sigma^2 \end{bmatrix}^{\frac{1}{2}}$$
 as loaded

A representative ultimate strength, S2, is calculated from:

(15)
$$S_2 = \left[\sigma_{bx}^2 + \sigma_{tx}^2 \right]^{\frac{1}{2}}$$
 at failure

where the failure state is the state at which

(16)
$$\begin{bmatrix} \sigma_{\text{bx}} \\ \sigma_{\text{tx}} \end{bmatrix}_{\text{failure}} = \begin{bmatrix} \sigma_{\text{bx}} \\ \sigma_{\text{tx}} \end{bmatrix}_{\text{loaded}}$$

Then, as shown in Fig. 30, the excess bearing capacity, B is defined as

(17)
$$B = \frac{S_2 - S_1}{S_1}$$

B > 0 at all holes in a joint implies that there is some margin of safety.

B = 0 at any hole in a joint implies that there is no margin of safety.

B < 0 at any hole in a joint implies that the joint would fail under the applied load.

The effect of laminate composition and bolt hole size on excess bearing capacity is shown in Figs. 31, 32, and 33.

C. DETERMINING THE WEIGHT OF A NON-BUFFER STRIP JOINT

The weights per inch of chord for the non-buffer strip joints were calculated by multiplying the cross-sectional

areas of each joint by the density of NARMCO 5208/T300 graphite-epoxy laminate material. The effect of laminate composition, hole size, and number of bolt holes upon joint weight is shown in Figs. 34, 35, and 36.

III. ANALYSIS OF THE BUFFER STRIP JOINT

A. SIZING THE BUFFER STRIP JOINT

Figure 37 is a schematic of the buffer strip joint design. All bolt holes are of the same diameter. Except for the inboard row, all bolt holes are placed in the buffer strips. This placement was chosen for two reasons:

- 1. It took advantage of the high bearing capacity of NARMCO 5208/T300 $\left[\pm45\right]$ laminates.
- It reduced stress concentrations in the heavily loaded primary strips.

The bolt holes in the buffer strips are spaced so that there is a distance of four hole diameters between adjacent hole centers. Two bolt holes are placed in each primary strip which is located between two buffer strips. These bolt holes are placed in a row with the inboard bolt in the buffer strip. In the joint analysis, wing taper is disregarded and the spanwise edges of the buffer and primary strips are considered parallel. It is assumed that joint thicknesses at any position are the same in the buffer and primary strips.

The buffer strips used in the joints analyzed in this study are four hole diameters wide, and the two primary

strips are each 3.335 hole diameters wide. This gives an overall buffer strip joint width of 10.67 hole diameters. These dimensions were chosen because it was felt that they were representative of a geometry which could be used in an advanced fighter type aircraft wing skin application. No attempt is made to justify these dimensions either analytically or experimentally, and no attempt is made to assess the effect of this choice of dimensions upon joint efficiency.

In the following theoretical development, as in the case of the non-buffer strip joint, a tensile load $N_{\rm X}$ and a shear load $N_{\rm XY}$ are assumed constant across the outboard edge of the joint. It is also assumed that fittings were designed so that each row of bolts in the joint transfers the same portion P of the applied tensile load and so that the shear load is reacted by the inboard row of bolts, each of the inboard bolts carrying an equal share of the shear load as well as a share of the tensile load. To utilize the high bearing capacity of a NARMCO 5208/T300 $\left[\pm 45\right]$ laminate, it was decided to impose a requirement that at the inboard row of bolts, the primary strips be composed of 100 per cent ± 45 degree plies.

Considering the joint sketched in Fig. 37, the load, L, on a single buffer strip joint, is given by:

(18)
$$L = N_AD$$

where AD is the overall joint width. The bolt load in all bolts except those in the inboard row is given by

(19)
$$P = \frac{L}{M} = \frac{N_{\chi}AD}{M}$$

where M is the number of rows of bolts in the joint.

Since the shear load $N_{\rm xy}$ and a total tensile bolt load P are reacted equally by each of the three bolts in the inboard row of bolts, the resultant load, R, on each of these bolts is calculated from

$$(20) \quad R^2 = \left[\frac{N_x AD}{3(M)}\right]^2 + \left[\frac{N_{xy} AD}{3}\right]^2$$

(21)
$$R = \frac{ADN_{X}}{3} \left[\left[\frac{1}{M} \right]^{2} + \left[\frac{N_{XY}}{N_{X}} \right]^{2} \right]^{\frac{1}{2}}$$

As in the non-buffer strip joint design, the desired interbolt strain level, 3000 micro-inches per inch, is the primary consideration determining the joint geometry for the buffer strip design. Locations in the joint are described by station numbers, just as in the non-buffer strip design. In the case of the buffer strip design, however, the station numbers vary from $\eta=1$, which corresponds to the location of the outboard bolt-hole center, to station $\eta=1$ which corresponds to the location of the row of centers of the inboard bolts.

The thickness at station $\eta=1.5$ is determined by the applied load, the joint geometry, the joint material composition, and the desired interbolt strain level. The average modulus of the joint, $E_{\rm Xave}$, as defined in Ref. 7, is used in calculating this thickness.

(22)
$$E_{x_{aye}} = \frac{D(A-W_B) E_{x_1} + W_BDE_{x_2}}{AD}$$

where W_BD = width of the buffer strip

 $\mathbf{E}_{\mathbf{x_1}}$ = tensile modulus of the primary strip

 $\mathbf{E}_{\mathbf{x}_2}$ = tensile modulus of the buffer strip

As shown in Fig. 4, E_{x_1} is determined by the percentage of zero degree plies in the primary laminate. As shown in Fig. 3, E_{x_2} varies with strain level.

The thickness at station η =1.5 is derived from

(23)
$$\epsilon = \frac{ADN_{X} \left[1 - \frac{1}{M}\right]}{ADt E_{X_{AVE}}}$$

where ϵ is the desired interbolt strain level. Thus,

(24)
$$t_{1.5} = \frac{AN_{x} \left[1 - \frac{1}{M}\right]}{\left[(A - W_{B})E_{x_{1}} + W_{B}E_{x_{2}}\right] \epsilon}$$

Similarly,

(25)
$$t_{M-.5} = \frac{AN_{x} \left[\frac{1}{M}\right]}{\left[(A-W_{B})E_{x_{1}}+W_{B}E_{x_{2}}\right] \in}$$

The bolt bearing stress in the inboard row of bolts is given by

(26)
$$\sigma_{BR} = \frac{R}{t^*}$$

where t*, the effective bearing thickness, is defined as in the non-buffer strip joint.

As stated earlier, the bearing strength of NARMCO 5208/T300 $\left[\pm45\right]$ degree laminates is 78000 lbf./in.². This determines the minimum allowable joint thickness at station

 η = M for any given load condition.

The laminate composition in the primary strips is initially assumed to vary linearly with distance from the composition at station $\eta = 1.5$, where it is the same as that of the plate outboard of the joint, to 100 per cent ± 45 degree plies at station $\eta = M$ where the applied shear loads are reacted.

The joint thickness at station $\eta = M-.5$ is determined by the desired interbolt strain level.

(27)
$$t_{M-.5} = \frac{AN_x}{M(A-W_B) E_{x_1} + W_B E_{x_2}} \epsilon$$

The remaining joint thicknesses are then determined geometrically from those at $\eta=1.5$ and $\eta=M-.5$ using the same techniques as for the non-buffer strip joint. If possible, a cross-section similar to that shown in Fig. 2(b) is used. When this yields a thickness at the last bolt which is too small, using the maximum bearing stress criteria discussed above and Eq. 26, a cross-section similar to that of Fig. 2(a) is used.

Having fixed the joint geometry, the laminate composition is determined by the requirement that the design strain level be maintained between each pair of bolt holes.

At any station $\eta = k+.5$, k=1, 2, ..., M-1,

(28)
$$\epsilon = \frac{N_{x}A\left[1-\frac{k}{M}\right]}{\left[E_{x}(A-W_{B}) + E_{x}W_{B}\right]t}$$

Since the composition of the buffer strips is fixed and $\mathbf{E}_{\mathbf{x}_2}$

is determined by the interbolt strain level, it is necessary to vary $\mathbf{E}_{\mathbf{x}_1}$ and hence the composition of the primary strips to maintain the desired strain level as the bypass loads in the joint vary from hole to hole.

(29)
$$E_{x_1} = \frac{1}{(A-W_B)} \left[\frac{N_x A \left[1-\frac{k}{M}\right]}{t_{\eta}} - W_B E_{x_2} \right]$$

It is assumed that $E_{\rm x_l}$ varies linearly with distance between stations η = k-.5 and η = k+.5. Thus

(30)
$$E_{x_{l_k}} = \frac{E_{x_{l_{k+,5}}} + E_{x_{l_{k-,5}}}}{2}$$

Determination of $\mathbf{E}_{\mathbf{x}_{\mathbf{l}_k}}$ determines the required percentage of zero degree plies in the primary laminate at station k.

Having determined the joint geometry and laminate composition, it is then possible to determine the joint weight and excess bearing capacity.

B. DETERMINING THE STRENGTH OF A BUFFER STRIP JOINT

The bolt load P is not carried entirely in the buffer strip. Part of it is transmitted, in shear, to the primary strips. This load splitting is shown in Fig. 38 in which P_1 is the portion of the bolt load P reacted through each of the primary strips and P_2 is the portion of P reacted through the buffer strip. The relationship between P_1 and P_2 is determined analytically as follows:

Referring to Fig. 38,

(31)
$$P = 2P_1 + P_2$$

The bypass strain levels in the buffer and primary strips

are assumed the same. Defining

$$(32) \quad 2W_1D = AD - W_BD$$

$$(33) \quad 2W_1 = (A - W_B)$$

(34)
$$\frac{P_1}{E_{x_1}W_1t} = \frac{P}{2E_{x_1}W_1t + E_{x_2}W_Bt}$$

Rearranging Eq. 34 gives an expression for P_1 in terms of P, the joint composition, and the joint geometry.

(35)
$$\frac{P_{1}}{P} = \frac{E_{x_{1}}W_{1}t}{2E_{x_{1}}W_{1}t + E_{x_{2}}W_{B}t}$$

This equation is rewritten in the form

(36)
$$P_1 = A_n P$$

where A_n is determined by knowledge of the joint laminate composition, geometry, and strain level.

(37)
$$A_n = \frac{E_{x_1}^{W_1}}{2E_{x_1}^{W_1} + E_{x_2}^{W_B}}$$

The bolt load splitting discussed above is dependent upon the ability of the ± 45 degree laminae to transfer a shear load, F_S , from the buffer to the primary strips. It was experimentally determined that failure of this load transferring mechanism could be expected when the shear stress in these fibers, f_S , reached a magnitude of 90,000 lbf./in.² (Ref. 9). At any station in the joint

(38)
$$F_{S_{\eta}} = \frac{P_1}{4Dt_{\pm 45}}$$
 ($\eta = integer$)

where $t_{\pm 45}$ is the total thickness of ± 45 degree laminae through which P_1 is transferred. Defining Z = percentage of zero degree plies in the primary strips,

(39)
$$t_{\pm 45} = t \frac{(100-Z)}{100}$$

(40)
$$f_{s\eta} = \frac{N_x A A_n}{4M t_{100-Z}}$$
 ($\eta = integer$)

The shear stress f_s varies from bolt to bolt in a given buffer strip joint design. In all designs, however, the highest values for f_s occur at the first bolt hole. Thus f_s determines the upper limit on the percentage of zero degree plies in the primary strip laminate. From Eq. 24,

$$(41) \quad t_{1} = \frac{AN_{x} \left[1 - \frac{1}{M}\right]}{\left[(A - W_{B})E_{x_{1}} + W_{B}E_{x_{2}}\right] \epsilon}$$

Fig. 4 yields the following relationship between laminate composition and modulus,

(42)
$$E_{x_1} = 10^6 \left[20.7 - (100 - Z) \left[\frac{20.7 - 2.8}{100} \right] \right] (1bf./in.^2)$$

Then,

(43)
$$\frac{100-Z}{100} = \left[20.7 - \frac{E_{x_1}}{10^6}\right] \frac{1}{17.9}$$

Substituting Eqs. 37, 41, and 43 into Eq. 40,

(44)
$$f_{s_1} = \frac{W_1 E_{x_1}}{(M-1)} \frac{1}{4} \frac{\epsilon_1}{\left[20.7 - \frac{E_{x_1}}{10^6}\right]} \frac{1}{17.9}$$

From Eq. 44 it is seen that f_S is determined by the joint

geometry, laminate composition, and design strain level. Fixing the joint geometry and the design strain level determines the maximum allowable modulus for the primary strips and hence provides an upper limit on the per cent zero degree plies which can be used in the primary strips. This limit is determined by setting f_{S_1} equal to its experimentally determined maximum, 90,000 lbf./in. 2 and using Eq. 45 to determine $E_{x_{l_{max}}}$

$$E_{x_{l_{max}}} = \frac{4(M-1)(20.7)f_{s_{l}}}{17.9(W_{l})(\epsilon_{l})10^{6} + 4(M-1)f_{s_{l}}} 10^{6}(lbf./in.^{2})$$

Under the design conditions applicable to this study, Eq. 45 implies an upper limit of 92 to 98 per cent zero degree plies in the primary strips.

Three other failure modes of a buffer strip joint were found to be most probable under $N_{\mathbf{x}}$ and $N_{\mathbf{x}\mathbf{y}}$ loading (Ref. 15). Type I and Type II failure occurred in the buffer strip at the loaded bolt holes. Type I failure was characterized by radial cracks at 45 degrees to the X axis. Type II failure was characterized by radial cracks originating at the edge of the hole at 90 degrees to the X axis. Type III failure occurred when the load bearing fibers in the primary strips were broken. These three failure modes are sketched in Fig. 39.

The Type I failure mode characterizes the interaction of bearing and shear stresses in the buffer strip. It was found to be essentially independent of the bypass

stress. The load curves describing this failure mode were derived from experimental results (Ref. 15). Single hole specimens of buffer strip joint material were clamped in test machines along either one or two sides as shown in Fig. 40. With the bolts torqued, the specimens were loaded, and the failure bolt load stresses measured. Tests were run for specimens with 0.25 inch and 0.4375 inch diameter holes. For the doubly clamped test cases Type I failure occurred under the following loads:

D = 0.250 in.
$$\sigma_{\text{bx}_{\text{max}}} = 151,200 \text{ lbf./in.}^2$$

D = 0.4375 in.
$$\sigma_{\text{bx}_{\text{max}}} = 144,100 \text{ lbf./in.}^2$$

For the test specimens clamped at only one edge, Type I failure occurred under the following loads:

D = 0.25 in.
$$\sigma_{\rm bx} = 111,000 \, {\rm lbf./in.}^2$$

$$D = 0.4375 \text{ in. } \sigma_{bx} = 107,000 \text{ lbf./in.}^2$$

Satisfactory test results for the pure shear load case could not be obtained.

An attempt was made to approximate the shear effects by superposition of the singly and doubly clamped test results. The finite element computer program ISANIS, listed in Appendix A, was used to analyze the stress concentration field in various orthotropic plates. It was found that for a square plate made from uniform material with a central hole and sides at least four hole diameters in length, the stress field at the hole due to pure applied

shear could be closely approximated by an appropriate superposition of the stress fields resulting from singly and doubly clamped load cases. The superposition used is shown schematically in Fig. 41. The key assumption in this superposition is that the moment reaction which is representative of the single clamped edge load case can be replaced by a couple of equal magnitude resulting from shear loads applied on the upper and lower edges of the specimen. This assumption is really an application of the St. Venant principle that points in a body removed from load application locations react to the load applied rather than its mechanism of application. ISANIS was used to test this assumption and, under the conditions stated above, it was found to be reasonable.

The test specimens were thin and hence t*=t. Therefore,

$$(46) P = \sigma_{bx} Dt$$

For the double clamped specimen, the reaction force, $\boldsymbol{F}_{\boldsymbol{R}_{D}}$ is given by

(47)
$$F_{R_D} = \frac{P}{2} = \frac{\sigma_{bx}Dt}{2}$$

Assuming that this force is uniformly distributed across the clamped edges, an edge stress is defined

(48)
$$\sigma_{R_D} = \frac{F_{R_D}}{\ell Dt}$$

where ℓ X D equals the length of the clamped edge.

For the single clamped specimen, the reaction force,

 $F_{R_{\mathbf{S}}}$, is equal to the applied bolt load P. The reaction moment, m, is given by

$$(49) \quad m = P \frac{\ell D}{2}$$

This moment is approximated by a couple of the same magnitude formed by forces acting on the edges of the specimen which are normal to the clamped edge. For square specimens of side length ℓD , the magnitude of these forces, F, is given by

$$(50)$$
 FLD = m

(51)
$$FLD = \frac{PLD}{2}$$

$$(52)$$
 F = $\frac{P}{2}$

This development is also shown schematically in Fig. 41.

Assuming that each force F is distributed uniformly along the specimen edge upon which it is applied, an edge shear is defined

(53)
$$\sigma_{xy} = \frac{F}{\ell Dt}$$

(54)
$$\sigma_{xy} = \frac{P}{2lDt}$$

For the test specimens each side was four hole diameters in length. From Eqs. 47 and 54, the superposition yields

(55)
$$\sigma_{xy} = \frac{\sigma_{bx}}{8}$$

Under these assumptions, the experimental data listed previously yield the following failure states:

$$\sigma_{xy} = 0 \qquad \qquad \sigma_{bx} = 151,200 \text{ lbf./in.}^2$$

$$\sigma_{xy} = 13,875 \text{ lbf./in.}^2 \qquad \sigma_{bx} = 111,000 \text{ lbf./in.}^2$$

$$D = 0.4375 \text{ in.}$$

$$\sigma_{xy} = 0 \qquad \qquad \sigma_{bx} = 144,100 \text{ lbf./in.}^2$$

$$\sigma_{xy} = 13,375 \text{ lbf./in.}^2 \qquad \sigma_{bx} = 107,000 \text{ lbf./in.}^2$$

Figure 42 was prepared from these data points assuming that the ultimate bearing stress-shearing stress interaction curve was linear for the graphite-epoxy laminates used in this study.

Buffer strip Type II failure curves were experimentally determined for buffer strip joint specimens with 0.4375 inch bolt holes, a buffer strip width of 1.5 inches, and primary strips each 1.25 inches wide (Ref. 15). The hole centers were spaced four diameters apart. These tests were run with primary strips composed of 30 per cent zero degree plies and 50 per cent zero degree plies with bolt loads applied through torqued bolts. These test specimens were thin enough so that t*=t. Tests were also run on buffer strips alone to determine the ultimate bypass stress of the buffer strip material (Ref. 15). With no applied bearing stress it was found that the ultimate bypass stress in the buffer strip material was 25000 lbf./in.2. The results of this series of tests indicated that the Type II failure mode for these test specimens could be closely described by the empirical relationship

(56)
$$\sigma_{\text{net buffer}} = \frac{P_2 + .25(2P_1)}{D(W_B - 1) t_2} + \sigma_{tx_{2net area}}$$

 $\sigma_{\rm net\ buffer}$ is the ultimate bypass stress in the buffer strip normalized to the width of the buffer strip minus the diameter of the bolt hole. $\sigma_{\rm tx_2}$ is the actual bypass stress in the buffer strip normalized to the width of the buffer strip minus the hole diameter. Thus,

(57)
$$\sigma_{\text{net buffer}_{\text{max}}} = 25000 \text{ lbf./in.}^2 (\frac{W_B}{W_B - 1})$$

(58)
$$\sigma_{\text{tx}_{2_{\text{net area}}}} = \frac{\sigma_{\text{tx}_{2}} w_{\text{B}}}{(w_{\text{B}}-1)}$$

Assuming that the strain levels in the buffer and primary strips are the same at any station η ,

$$(59) \quad \frac{\sigma_{tx_1}}{E_{x_1}} = \frac{\sigma_{tx_2}}{E_{x_2}} = \epsilon$$

Thus,

(60)
$$\sigma_{\text{tx}_{2_{\text{net}}}} = \frac{\sigma_{\text{tx}_{1}}}{E_{x_{1}}} E_{x_{2}} \frac{W_{B}}{(W_{B}-1)}$$

(61)
$$\sigma_{\text{bx}} = \frac{P}{Dt}$$

(62)
$$25000 \left(\frac{W_{B}}{W_{B}-1}\right) = \frac{\sigma_{bx}(1-1.5 A_{n})}{(W_{B}-1)} + \frac{\sigma_{tx_{1}} E_{x_{2}}}{E_{x_{1}}} \frac{W_{B}}{(W_{B}-1)}$$

For a fixed laminate composition in the primary strips, different values of $\sigma_{\rm tx}$ produce different strain levels. This implies variation in E2, the modulus of the buffer

strip material, with bypass stress in the primary strips. This variation in modulus explains why the Type II failure is not linear in $\sigma_{\rm bx}$ and $\sigma_{\rm tx_1}$.

Type III failure is characterized by fracture of the zero degree fibers in the primary strips. As reported in Ref. 2, this failure mode is encountered when the strain level in these strips reaches 10,000 micro-inches per inch. This failure mode is mathematically predicted by considering the presence of both the bypass stress and the stress due to P_1 in the primary strips. Thus,

(63)
$$\sigma_{\text{tx}_1} + \frac{A_n P}{W_1 D_t} = \sigma_1$$

(64)
$$\sigma_{\text{lult}} = \epsilon_{\text{ult}} E_{\text{l}}$$

(65)
$$P = \sigma_{bx} Dt^*$$

(66)
$$\sigma_{\text{tx}_1} + \frac{A_n \sigma_{\text{bx}} Dt^*}{(A-W_B) Dt} = \epsilon_{\text{ult}} E_1$$

The results of these tests are summarized in Fig. 43. The Type I failure line is drawn for a zero shear case and is determined from experiment with a double clamped test specimen, the Type II failure lines are drawn from Eq. 62, and the Type III failure lines are drawn from Eq. 66. For the joints used in this study, Eq. 62 becomes

(67)
$$\frac{\sigma_{\text{bx}}(1-1.5A_{\text{n}})}{3} + \sigma_{\text{tx}_{1}} = \frac{E_{\text{x}_{2}}}{E_{\text{x}_{1}}} + \frac{4}{3} = 25 + \frac{4}{3}$$

and Eq. 66 becomes

(63)
$$\sigma_{\text{tx}_1} + \frac{A_n \sigma_{\text{bx}}}{6.67} = \epsilon_{\text{ult}} E_1$$

Figures 44 and 45 describe the expected failure states for the buffer strips used in the study joints. The Type I failure lines on these figures are taken from the zero shear ultimate bearing stresses indicated on Fig. 42. The Type II and Type III failure lines shown in these figures are drawn from Eqs. 67 and 68.

Excess bearing capacity calculations were made for buffer strip joints just as had been done for non-buffer strip joints. In the case of the buffer strip joints, however, only 0.25 and 0.4375 inch holes were considered since Type I failure test data was available only for these hole sizes. The results of these calculations are presented in Figs. 46 and 47.

C. DETERMINING THE WEIGHT OF A BUFFER STRIP JOINT

The weight per inch of chord of each buffer strip design was calculated just as had been done for the non-buffer strip joints by multiplying the cross-sectional area of each joint by the density of the NARMCO 5208/T300 graphite-epoxy material used in the study. The variation of joint weight with primary strip laminate composition, bolt hole size, and number of bolts is shown in Figs. 48 and 49.

IV. DISCUSSION OF RESULTS

A. NON-BUFFER STRIP JOINTS

The following generalizations about non-buffer strip joints were found to be valid:

- 1. For a given hole size, the joint weight decreased as the percentage of zero-degree plies in the joint increased.
- 2. For a given hole size, the fewer the number of bolt holes per unit chord, the lighter the joint.
- 3. The smaller the bolt holes, the lighter the joint could be made.
- 4. The smaller the bolt holes, the greater the range in number of allowable bolt holes per unit chord.
- 5. For a given laminate composition, the smaller the bolt holes the larger the minimum number of bolt holes per unit chord required.
- 6. The smaller the bolt holes, the larger the allowable range of laminate composition.
- 7. For a given laminate composition, the smaller the bolt holes, the larger the excess bearing capacity.

B. BUFFER STRIP JOINTS

Observations 1-6, above, are also true for buffer strip joints. The excess bearing capacity of the buffer

strip joint, as seen in Figs. 48 and 49, is, in a gross sense, independent of hole size and more heavily influenced by laminate composition, the number of holes, and the load condition.

C. COMPARISON OF NON-BUFFER STRIP AND BUFFER STRIP JOINTS In Ref. 16 it is explained that the bearing strength of bolted plates is higher when the bearing loads are applied through torqued bolts than when they are applied through untorqued bolts. Since the failure modes of the buffer strip joints were derived from experiments in which the bolt loads were applied through torqued bolts, and since the failure modes of the non-buffer strip joints were derived from experiments in which the bearing loads were applied through untorqued bolts, this may explain at least part of the apparently higher excess bearing capacities available with buffer strip joints. Buffer strip joints generally weigh more than non-buffer strip joints. The fact that buffer strip joints require fewer bolts per inch of chord than non-buffer strip joints can be used to offset some of this weight difference if bolt weights are included in the net joint weight. The reduced number of bolts per inch of chord possible with buffer strip joints should also reduce joint fabrication costs by reducing the number of drilling operations required. Buffer strip joints can be constructed for a larger range of laminate composition than non-buffer strip joints.

V. CONCLUSIONS AND RECOMMENDATIONS

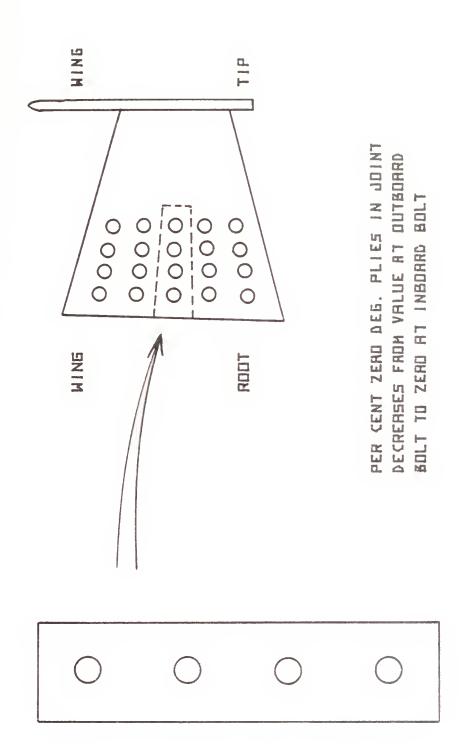
The design methodology used in this study is shown to be capable of producing workable joint designs. The wide range of weights and excess bearing capacities exhibited by the different joint designs indicates that the joint efficiencies achieved by geometric substitution of advanced composites for conventional structural materials were probably minimal when compared with those which would be achieved by designs which took advantage of the special high strength and high modulus properties of advanced composites.

Under the design conditions adopted in this study, buffer strip joints were found to be stronger and more cheaply manufactured than non-buffer strip joints. These advantages are offset by the increased joint weights characteristic of buffer strip joints. In spite of this weight penalty, it is felt that the high excess bearing capacity and integral crack stoppage capability of buffer strip joints makes them promising candidates for aerospace applications.

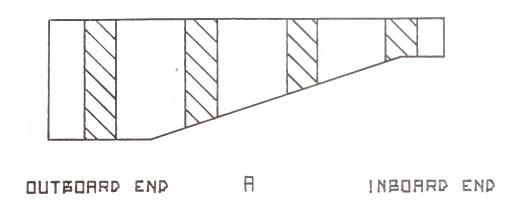
It is felt that Figs. 31-36 and 46-49 can be used to compare various design proposals and to estimate the costs of variation in laminate composition, hole size, or number of holes. No attempt was made to determine the effect of the design limitations summarized in TABLE I which were placed upon allowable joint geometry and

composition by such factors as manufacturing considerations and fitting interface requirements. It is recommended that the effect of these restrictions be determined by an analysis similar to this one with the restrictions removed.

It is recommended that application of the buffer strip technique to critical components be preceded by further experimentation to more accurately determine the behavior of buffer strip joints under shear loads.



SCHEMATIC OF A WING WITH A NON-BUFFER STRIP JOINT FIGURE 1.



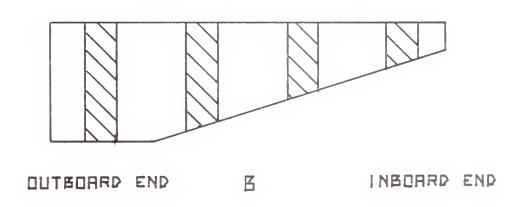


FIGURE 2. PERMISSIBLE JOINT CROSS SECTIONS

VARIATION OF SECANT MODULUS WITH STARIN OF NARM CO 5208/T300 (±45 Deg.) LAMINATED MATERIAL AT ROOM TEMPERATURE

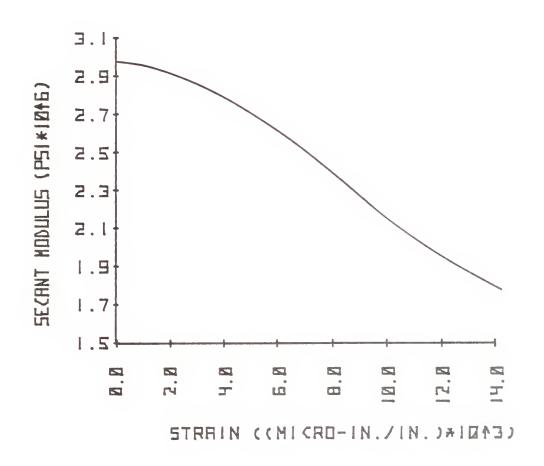


FIGURE 3. VARIATION OF SECANT MODULUS WITH STRAIN OF NARMCO 5208/T300 (±45 DEG.) LAMINATED MATERIAL AT ROOM TEMPERATURE

NARMOD 5208/T300 (0/±45) LAMINATES ECSECANT MODULUS) VS. PERCENT ZERO DEGREE PLIES

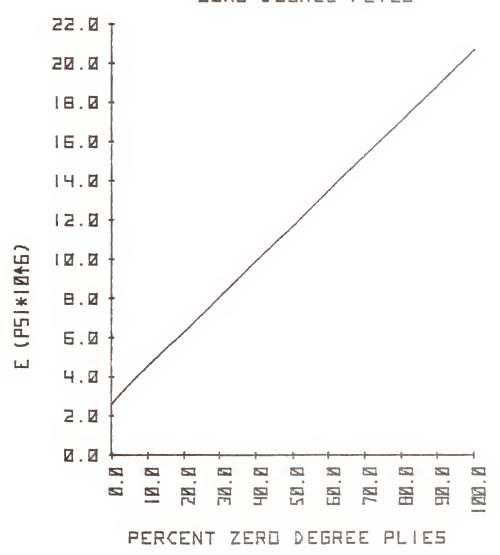
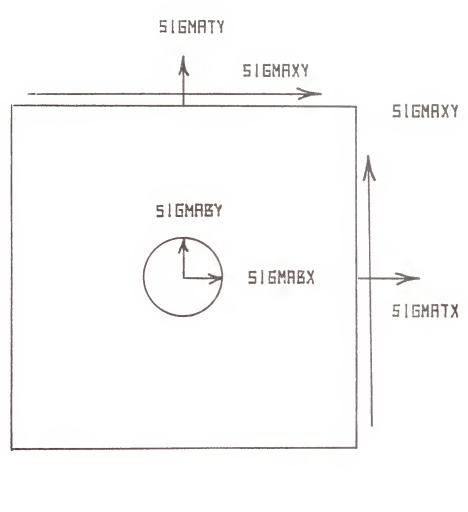


FIGURE 4. SECANT MODULUS OF NARMCO 5208/T300 [0/±45]
LAMINATES VS. PER CENT ZERO DEGREE PLIES



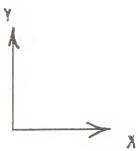


FIGURE 5. BOLTED JOINT APPLIED STRESS DEFINITIONS



0.25 IN. DIAM. HOLE 10% ZERO DEG. PLIES

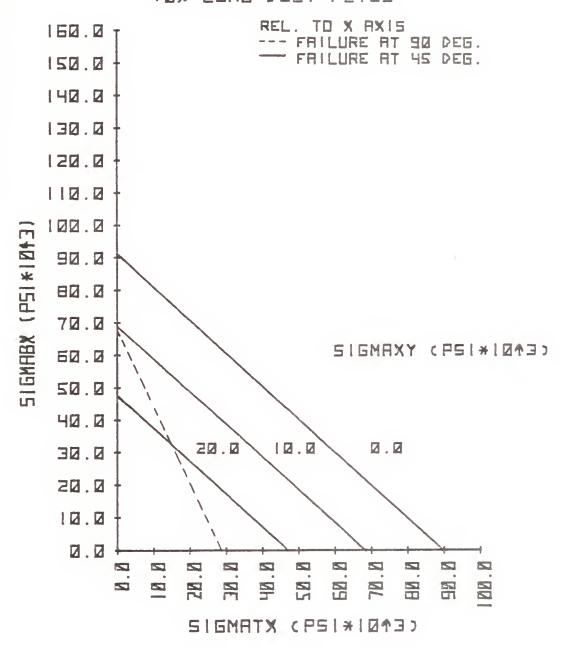


FIGURE 6. ULTIMATE STRESS INTERACTION CURVE FOR A
ONE IN. SQUARE PLATE OF NARMCO 5209/T300 [0/±45]

MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 10

PER CENT ZERO DEGREE PLIES

0.25 IN. DIAM. HOLE 20% ZERO DEG. PLIES

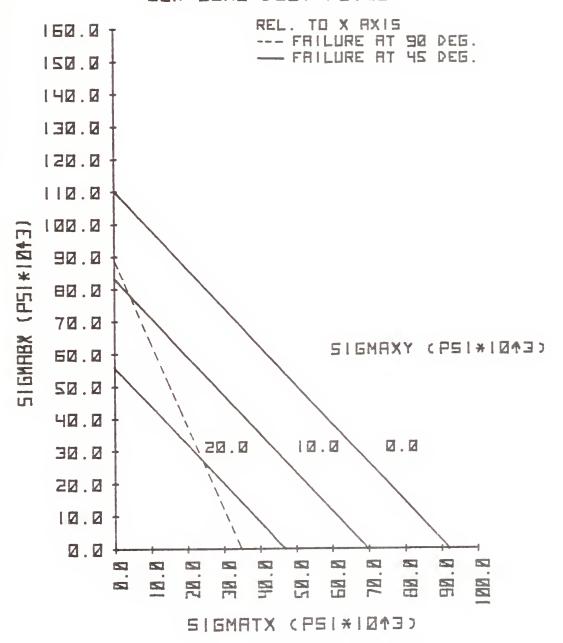


FIGURE 7. ULTIMATE STRESS INTERACTION CURVE FOR A ONE IN. SQUARE PLATE OF NARMCO 5203/T300 $\left[0/\pm45\right]$ MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 20 PER CENT ZERO DEGREE PLIES

0.25 IN. DIRM. HOLE 30% ZERO DEG. PLIES

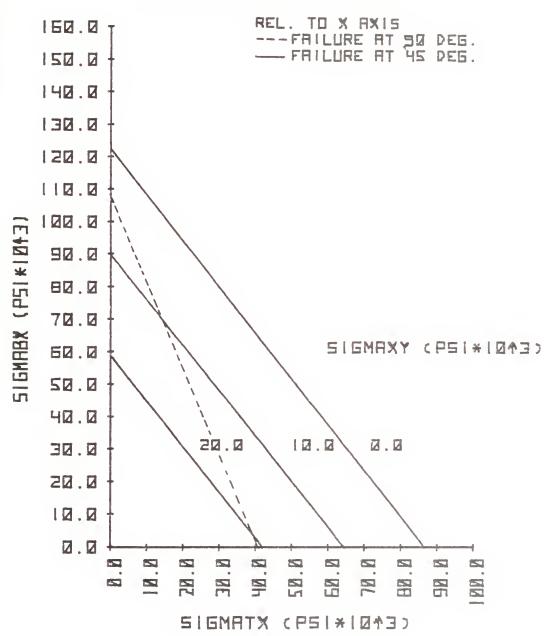


FIGURE 8. ULTIMATE STRESS INTERACTION CURVE FOR A ONE IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 30

PER CENT ZERO DEGREE PLIES

0.25 IN. DIAM. HOLE 40% ZERO DEG. PLIES

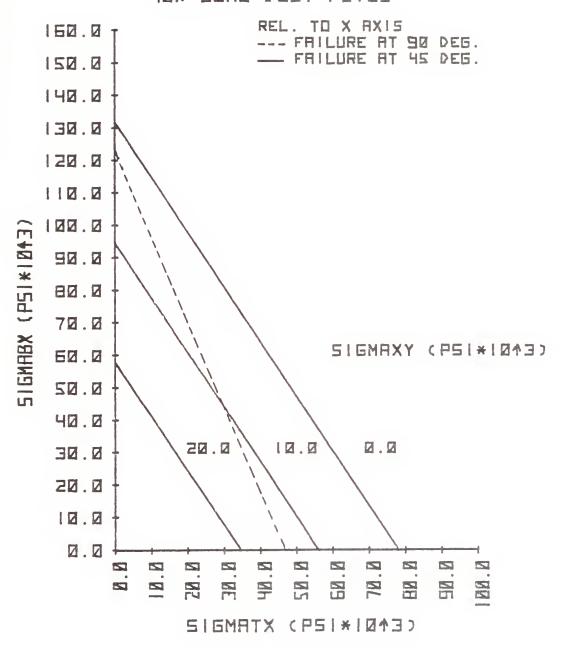


FIGURE 9. ULTIMATE STRESS INTERACTION CURVE FOR A

ONE IN. SQUARE PLATE OF NARMCO 5209/T300 [0/±45]

MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 40

PER CENT ZERO DEGREE PLIES

0.25 IN. DIRM. HOLE 50% ZERO DEG. PLIES

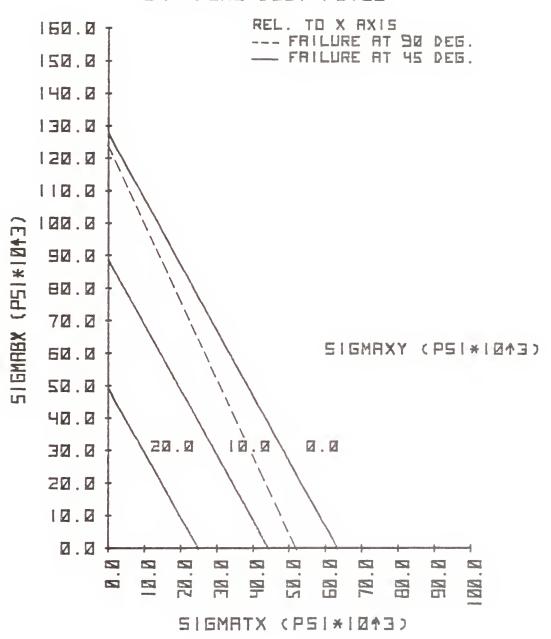


FIGURE 10. ULTIMATE STRESS INTERACTION CURVE FOR A

ONE IN. SQUARE PLATE OF NARMCO 5203/T300 [0/±45]

MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 50

PER CENT ZERO DEGREE PLIES

0.25 IN. DIAM. HOLE 60% ZERO DEG. PLIES REL. TO X AXIS 160.0 FRILURE AT FRILURE AT 90 DEG. 150.0 140.0 130.0 120.0 110.0 100.0 90.0 80.0 SIGNABA (PSI* (DIS) 70.0 60.0 50.0 40.0 30.0 20.0 12.2

0.0

FIGURE 11. ULTIMATE STRESS INTERACTION CURVE FOR A
ONE IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]
MATERIAL WITH A 0.25 IN. DIAMETER CENTRAL HOLE AND 60
PER CENT ZERO DEGREE PLIES

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SIGNATX (PSIALDAS)

D/

70

0.375 IN. DIRM. HOLE 10% ZERD DEG. PLIES

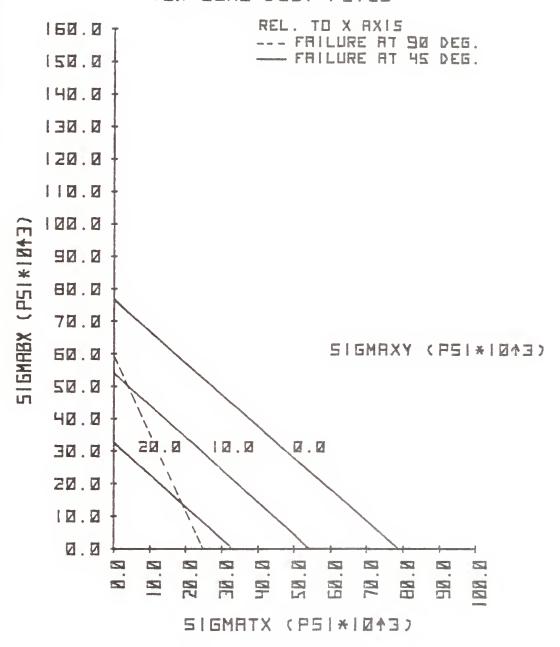


FIGURE 12. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

10 PER CENT ZERO DEGREE PLIES

0.375 IN. DIAM. HOLE 20% ZERO DEG. PLIES

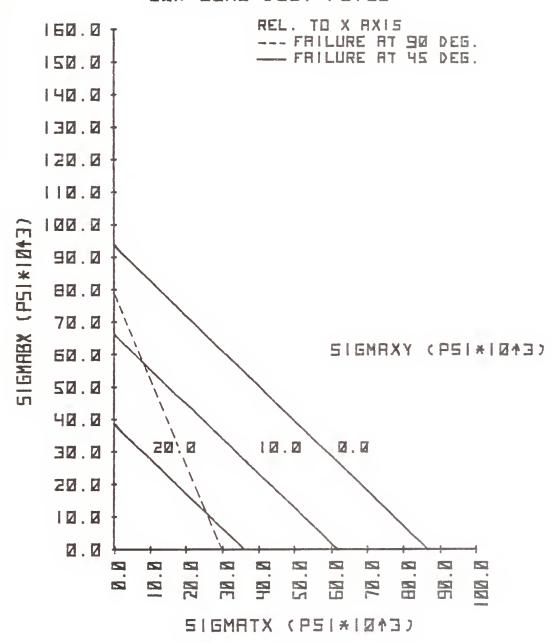


FIGURE 13. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

20 PER CENT ZERO DEGREE PLIES



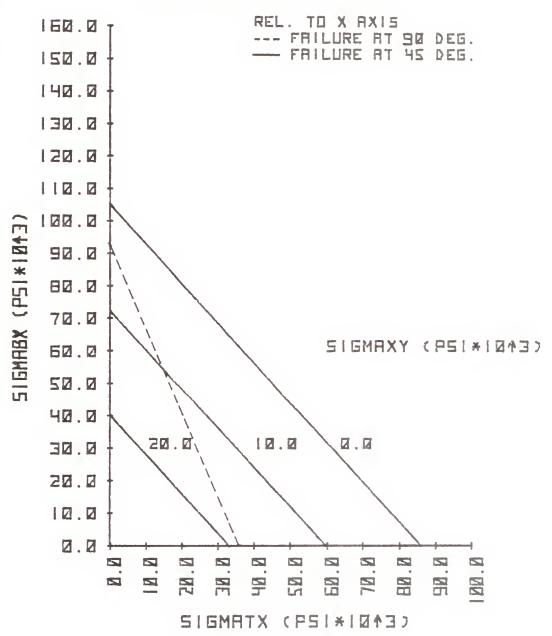


FIGURE 14. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

30 PER CENT ZERO DEGREE PLIES



0.375 IN. DIRM. HOLE 40% ZERO DEG. PLIES

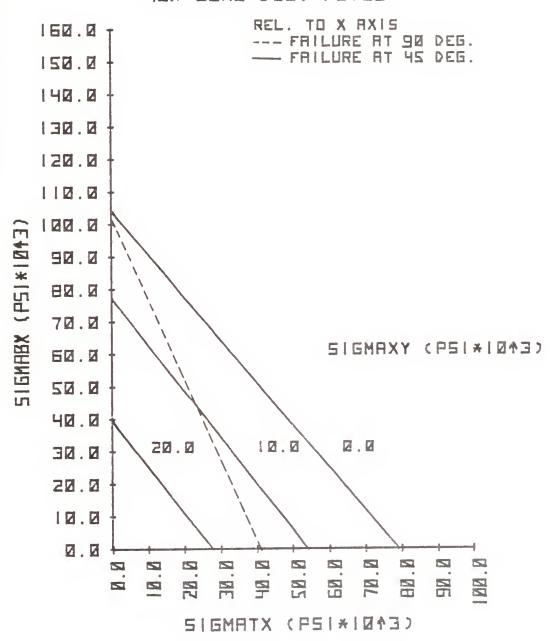


FIGURE 15. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

40 PER CENT ZERO DEGREE PLIES

0.375 IN. DIRM. HOLE 50% ZERO DEG. PLIES

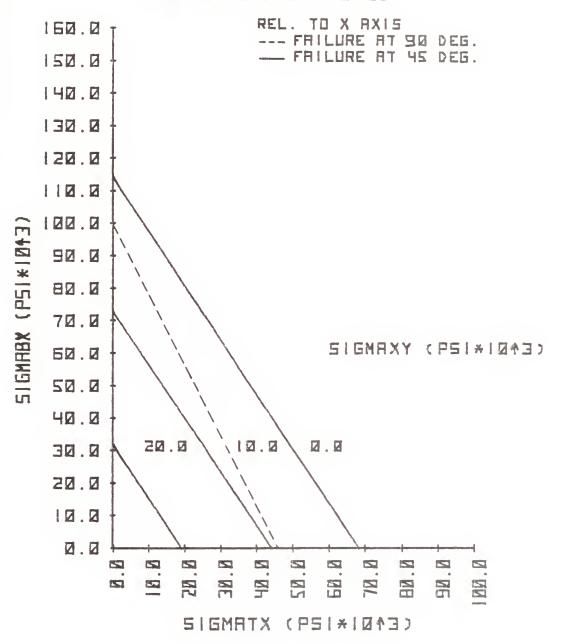


FIGURE 16. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

50 PER CENT ZERO DEGREE PLIES



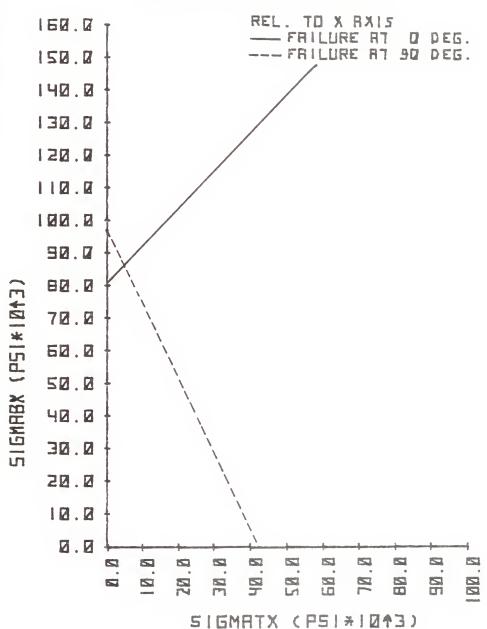


FIGURE 17. ULTIMATE STRESS INTERACTION CURVE FOR A

1.5 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.375 IN. DIAMETER CENTRAL HOLE AND

60 PER CENT ZERO DEGREE PLIES

0.4375 IN. DIAM. HOLE 10% ZERO DEG. PLIES

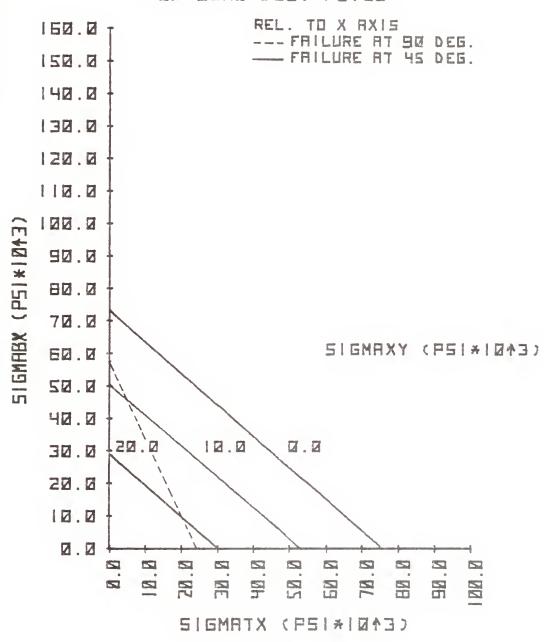


FIGURE 18. ULTIMATE STRESS INTERACTION CURVE FOR A 1.75 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45] MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND 10 PER CENT ZERO DEGREE PLIES

Ø.4375 IN. DIAM. HOLE 20% ZERO DEG. PLIES

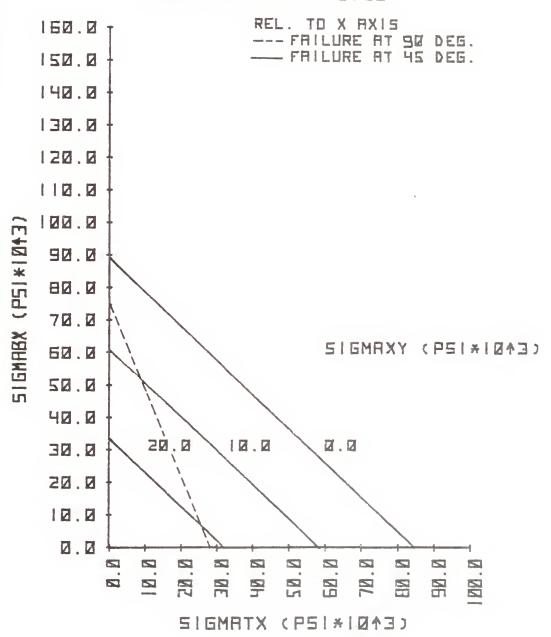


FIGURE 19. ULTIMATE STRESS INTERACTION CURVE FOR A

1.75 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND

20 PER CENT ZERO DEGREE PLIES

0.4375 IN. DIAM. HOLE 30% ZERO DEG. PLIES

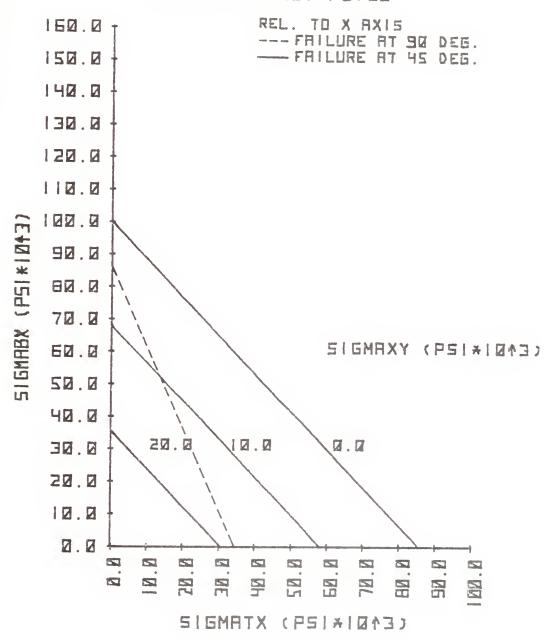


FIGURE 20. ULTIMATE STRESS INTERACTION CURVE FOR A

1.75 IN. SQUARE PLATE OF NARMCO 5209/T300 [0/±45]

MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND

30 PER CENT ZERO DEGREE PLIES

0.4375 IN. DIRM. HOLE 40% ZERO DEG. PLIES

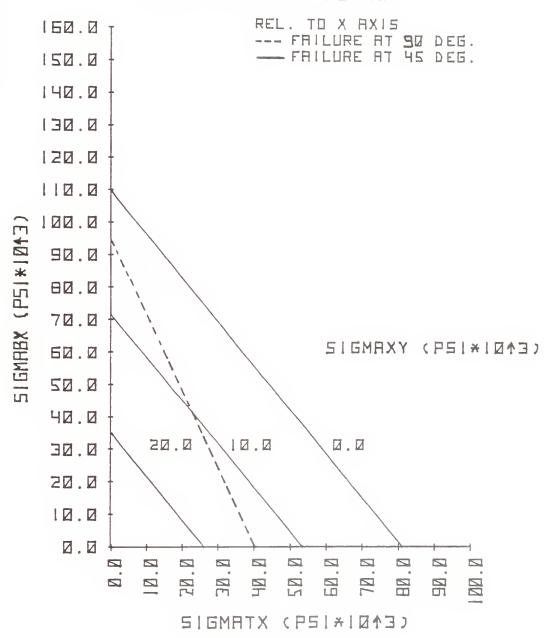


FIGURE 21. ULTIMATE STRESS INTERACTION CURVE FOR A

1.75 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND

40 PER CENT ZERO DEGREE PLIES

Ø.4375 IN. DIRM. HOLE 50% ZERO DEG. PLIES

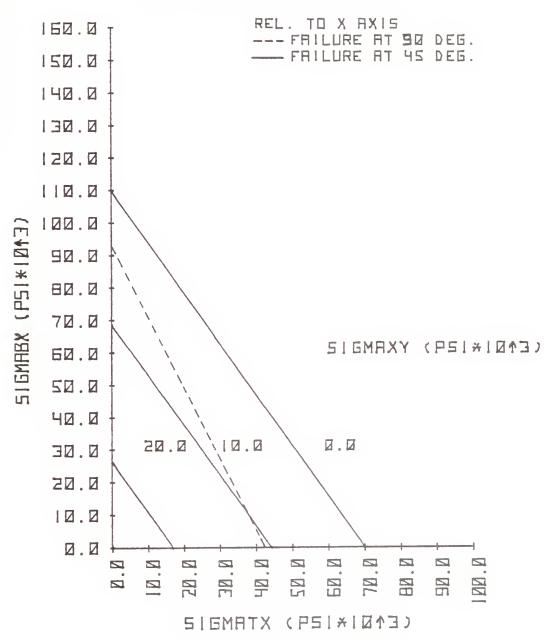


FIGURE 22. ULTIMATE STRESS INTERACTION CURVE FOR A 1.75 IN. SQUARE PLATE OF NARMCO 5209/T300 [0/±45] MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND 50 PER CENT ZERO DEGREE PLIES

0.4375 IN. DIRM. HOLE 60% ZERO DEG. FLIES

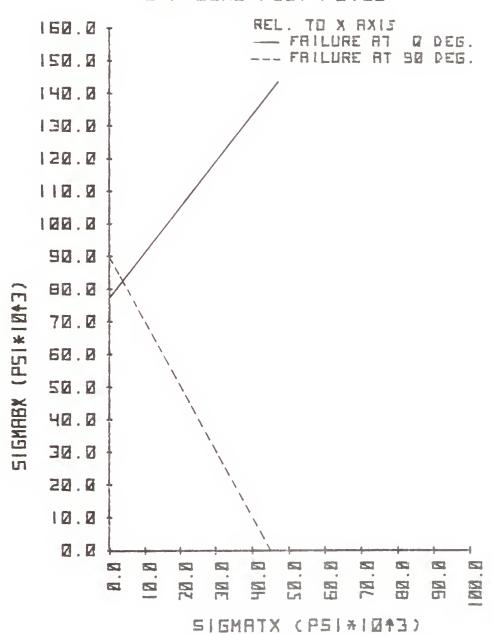


FIGURE 23. ULTIMATE STRESS INTERACTION CURVE FOR A 1.75 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.4375 IN. DIAMETER CENTRAL HOLE AND 60 PER CENT ZERO DEGREE PLIES



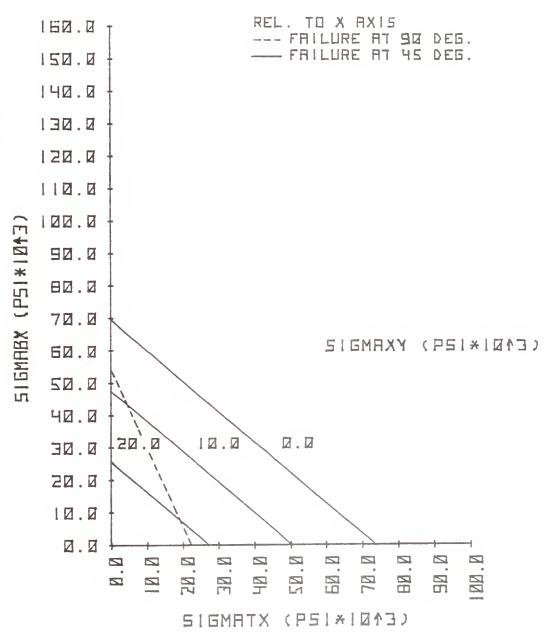


FIGURE 24. ULTIMATE STRESS INTERACTION CURVE FOR A

2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 10

PER CENT ZERO DEGREE PLIES

0.5 IN. DIAM. HOLE 20% ZERO DEG. PLIES

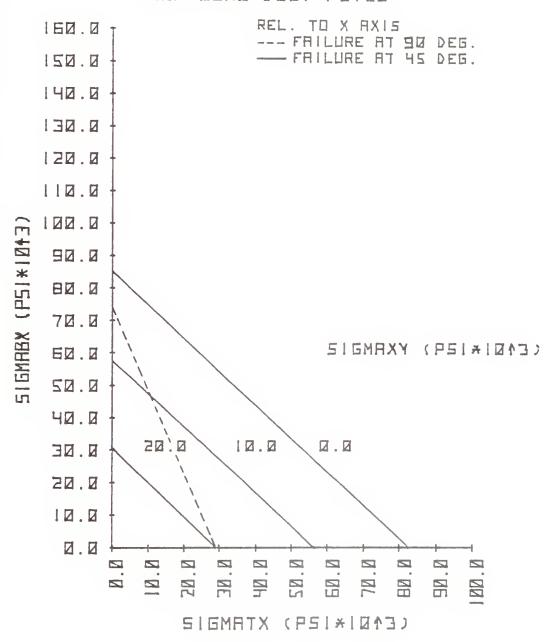


FIGURE 25. ULTIMATE STRESS INTERACTION CURVE FOR A

2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 20

PER CENT ZERO DEGREE PLIES

0.5 IN. DIRM. HOLE 30% ZERO DEG. PLIES

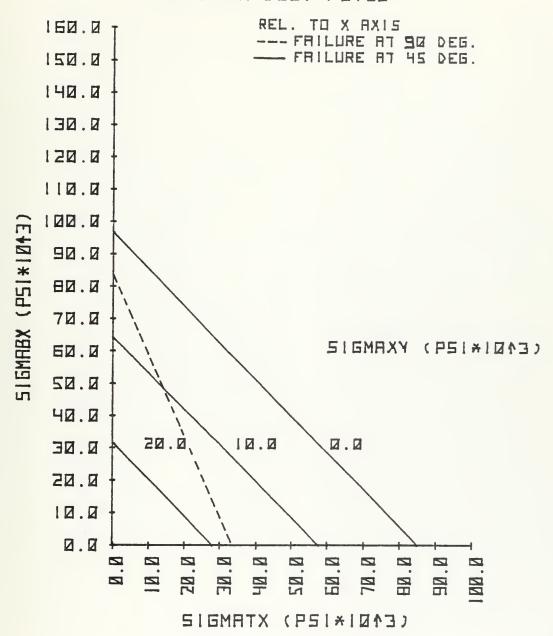


FIGURE 26. ULTIMATE STRESS INTERACTION CURVE FOR A

2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 30

PER CENT ZERO DEGREE PLIES

0.5 IN. DIAM. HOLE 40% ZERO DEG. PLIES

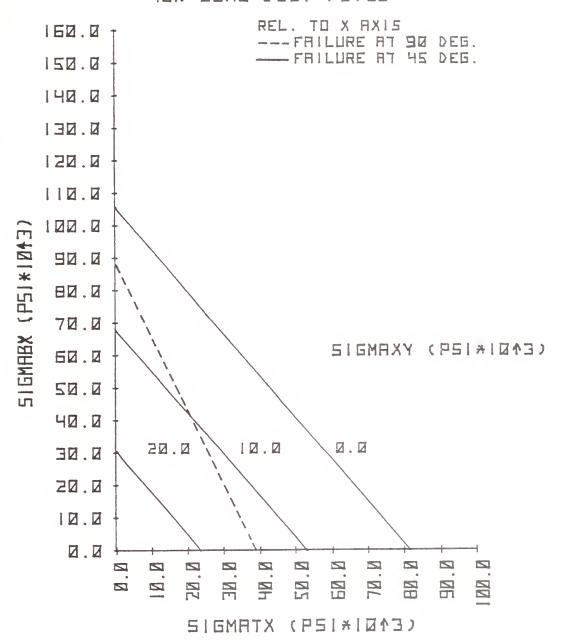


FIGURE 27. ULTIMATE STRESS INTERACTION CURVE FOR A
2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 40

PER CENT ZERO DEGREE PLIES



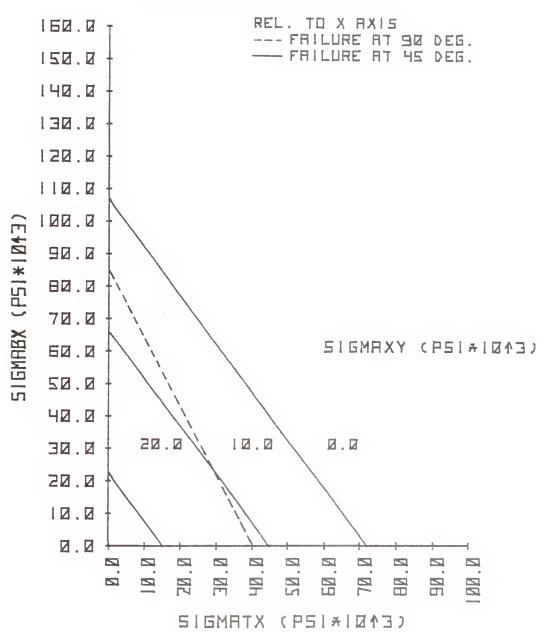


FIGURE 28. ULTIMATE STRESS INTERACTION CURVE FOR A

2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 50

PER CENT ZERO DEGREE PLIES

0.500 IN. DIAM. HOLE 60% ZERO DEG. PLIES

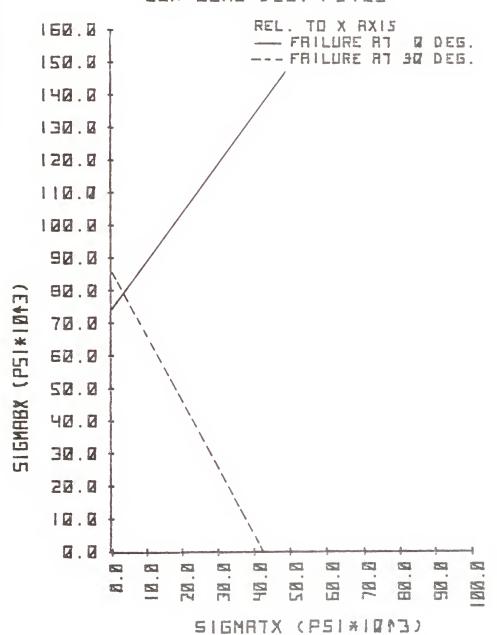


FIGURE 29. ULTIMATE STRESS INTERACTION CURVE FOR A

2.0 IN. SQUARE PLATE OF NARMCO 5208/T300 [0/±45]

MATERIAL WITH A 0.5 IN. DIAMETER CENTRAL HOLE AND 60

PER CENT ZERO DEGREE PLIES

EXCESS BERRING CAPACITY CALCULATIONS

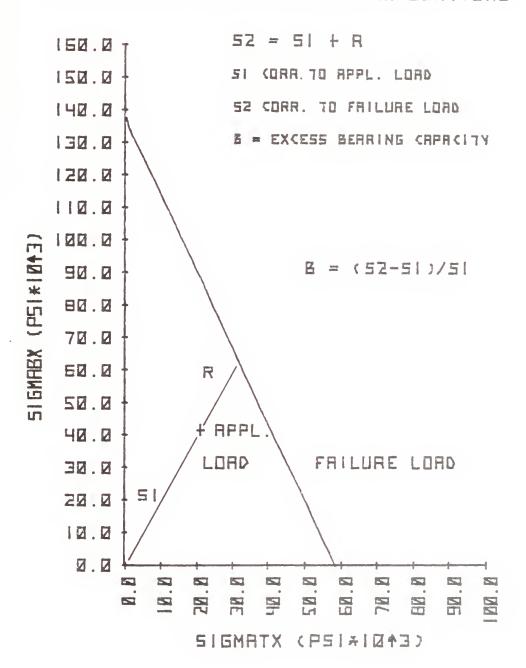
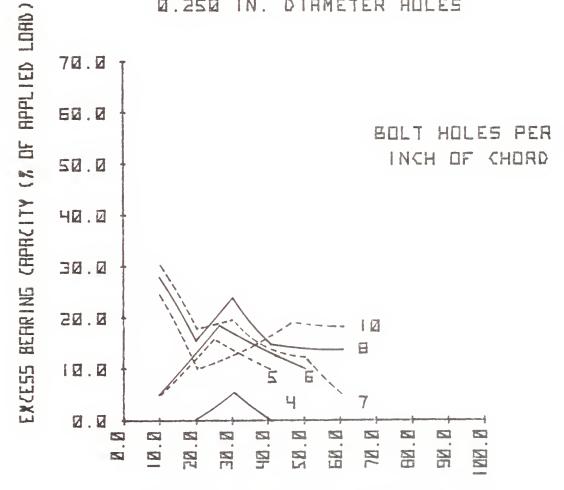


FIGURE 30. EXCESS BEARING CAPACITY CALCULATIONS

VARIATION OF EXCESS BEARING CAPACITY
WITH LAMINATE COMPOSITION
NON-BUFFER STRIP JOINT
0.250 IN. DIRMETER HOLES

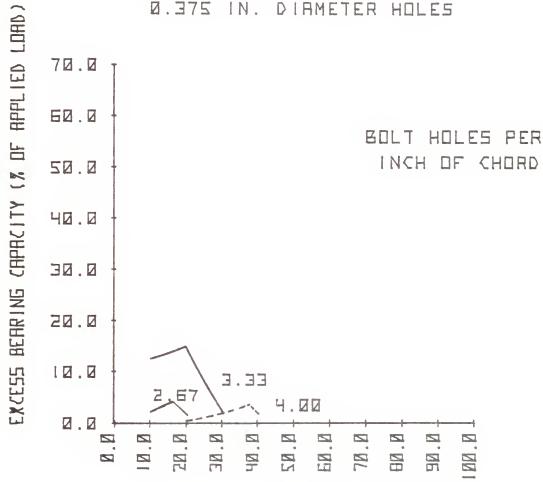


PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

FIGURE 31. VARIATION OF EXCESS BEARING CAPACITY WITH LAMINATE COMPOSITION FOR NON-BUFFER STRIP

JOINTS WITH 0.25 IN. DIAMETER BOLT HOLES

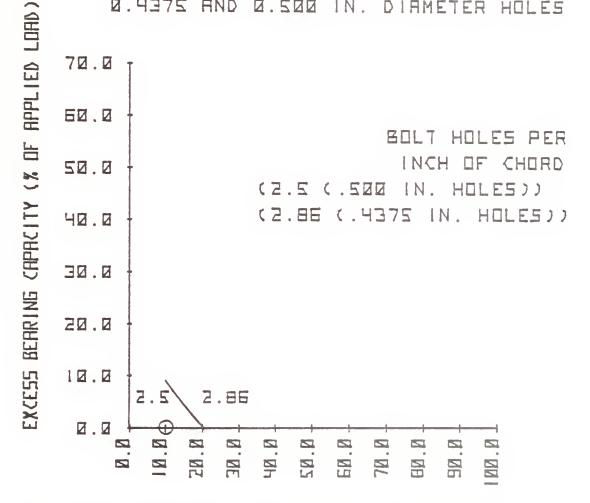
VARIATION OF EXCESS BEARING CAPACITY
WITH LAMINATE COMPOSITION
NON-BUFFER STRIP JOINT
Ø.375 IN. DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

FIGURE 32. VARIATION OF EXCESS BEARING CAPACITY
WITH LAMINATE COMPOSITION FOR NON-BUFFER STRIP
JOINTS WITH 0.375 IN. DIAMETER BOLT HOLES

VARIATION OF EXCESS GERRING CAPACITY
WITH LAMINATE COMPOSITION
NON-BUFFER STRIP JOINT
2.4375 AND 2.522 IN. DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

FIGURE 33. VARIATION OF EXCESS BEARING CAPACITY
WITH LAMINATE COMPOSITION FOR NON-BUFFER STRIP
JOINTS WITH 0.4375 AND 0.5 IN. DIAMETER BOLT HOLES

VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION

2.25 IN. DIAMETER HOLES

NON-BUFFER STRIP JOINT

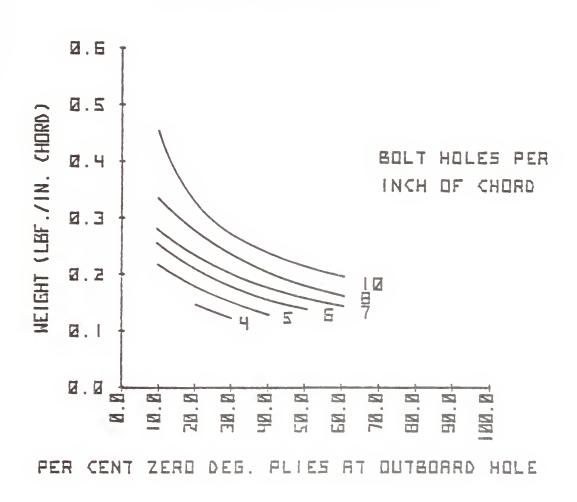


FIGURE 34. VARIATION OF JOINT WEIGHT WITH LAMINATE

COMPOSITION FOR NON-BUFFER STRIP JOINTS WITH 0.25

IN. DIAMETER BOLT HOLES

VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION

2.375 IN. DIAMETER HOLES

NON-BUFFER STRIP JOINT

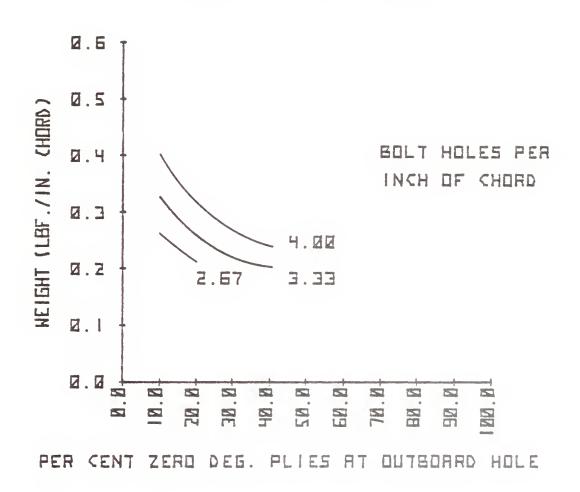
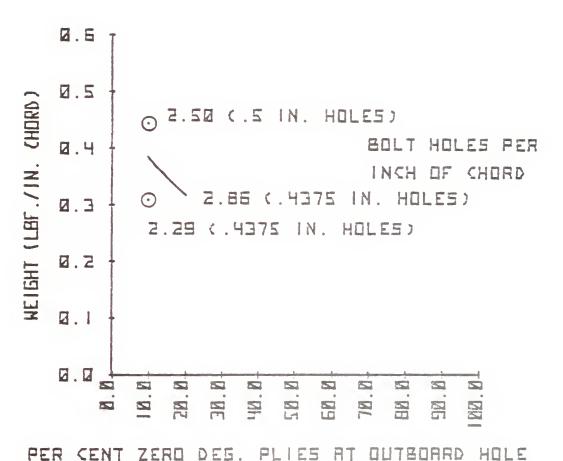


FIGURE 35. VARIATION OF JOINT WEIGHT WITH LAMINATE

COMPOSITION FOR NON-BUFFER STRIP JOINTS WITH 0.375

IN. DIAMETER BOLT HOLES

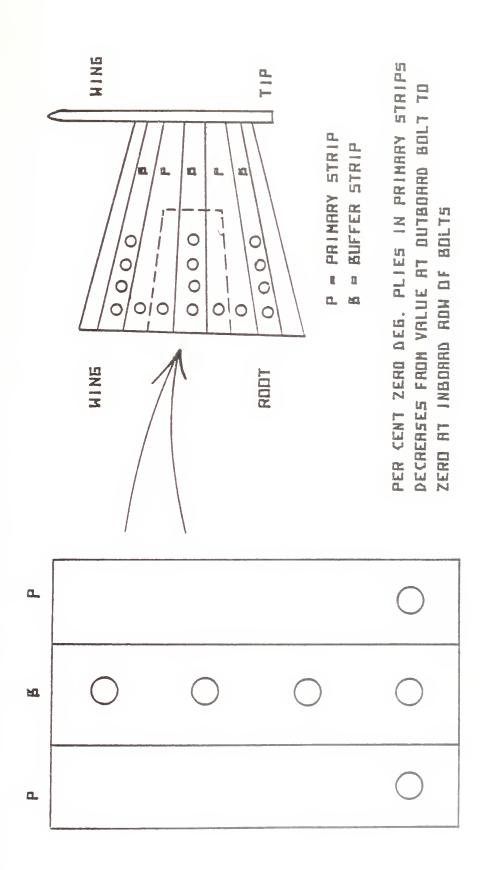
VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION 2.4375 AND 0.500 IN. DIAMETER HOLES NON-BUFFER STRIP JOINT



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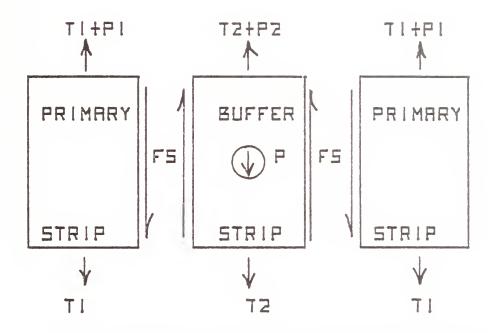
FIGURE 36. VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION FOR NON-BUFFER STRIP JOINTS WITH 0.4375

AND 0.5 IN. DIAMETER BOLT HOLES



SCHEMATIC OF A WING WITH A BUFFER STRIP JOINT FIGURE 37.

MECHANISM BY WHICH BOLT LOADS ARE REACTED IN A BUFFER STRIP JOINT



TI = TENSILE LOAD IN PRIMARY STRIP

T2 = TENSILE LOAD IN BUFFER STRIP

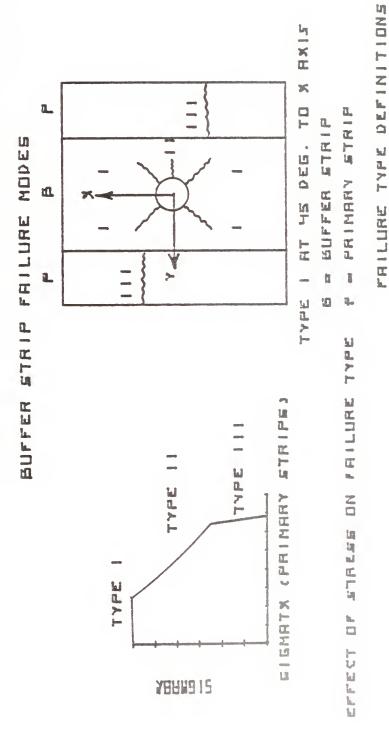
P = BOLT LOAD APPLIED AT HOLE

PI = BOLT LORD REACTED IN PRIMARY STRIP

P2 = BOLT LOAD REACTED IN BUFFER STRIP

FS = SHEAR PASSING PI 70 PRIMARY STRIP

FIGURE 38. MECHANISM BY WHICH BOLT LOADS ARE REACTED IN A BUFFER STRIP JOINT



DESCRIPTION OF THE EXPECTED BUFFER STRIP FAILURE MODES FIGURE 39.

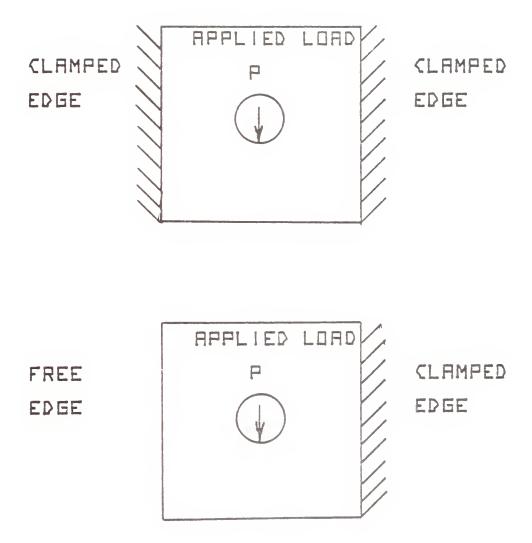


FIGURE 40. SCHEMATIC OF SHEAR LOADING TEST SPECIMENS

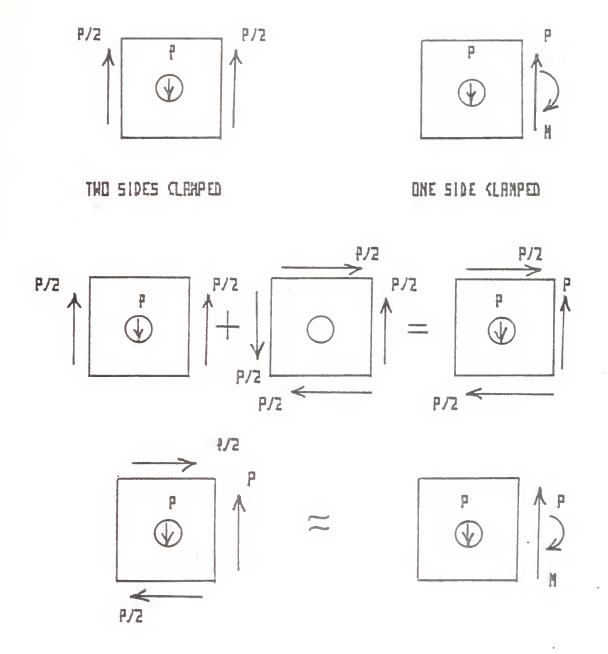


FIGURE 41. SCHEMATIC OF THE SUPERPOSITION USED TO

DETERMINE SHEAR EFFECTS ON A BUFFER STRIP

WITH A CENTRAL HOLE

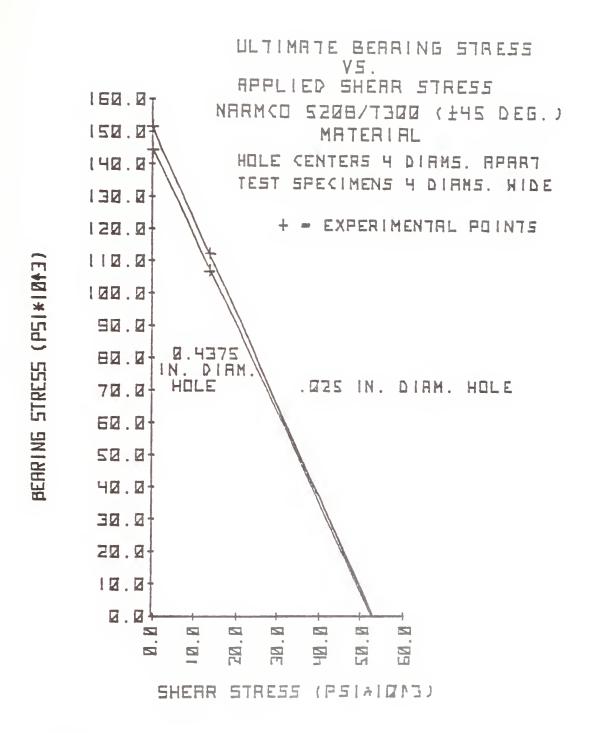


FIGURE 42. ULTIMATE BEARING STRESS-SHEAR STRESS
INTERACTION CURVE FOR A FOUR HOLE DIAMETER

SQUARE PLATE OF NARMCO 5203/T300 [±45]

MATERIAL WITH A CENTRAL HOLE



VARIATION OF ULTIMATE BEARING STRESS
WITH BYPASS STRESS IN THE PRIMARY
STRIPS - BUFFER STRIP JOINT

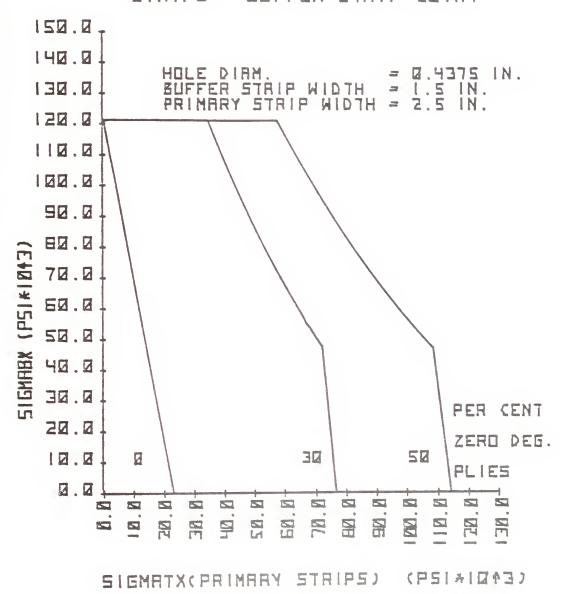


FIGURE 43. ULTIMATE STRESS INTERACTION CURVE FOR A BUFFER STRIP JOINT MADE FROM NARMCO 5208/T300 $\left[0/\pm45\right]$ MATERIAL WITH 2.5 IN. WIDE PRIMARY STRIPS, A 1.5 IN. WIDE BUFFER STRIP, AND A 0.4375 IN. DIAMETER CENTRAL HOLE

VARIATION OF ULTIMATE BEARING STRESS
WITH BYPASS STRESS IN THE PRIMARY
STRIPS - BUFFER STRIP JOINT

HOLE DIAM. # 0.250 IN.
BUFFER STRIP WIDTH # 4.00 DIAM.
PRIMARY STRIP WIDTH # 3.33 DIAM.

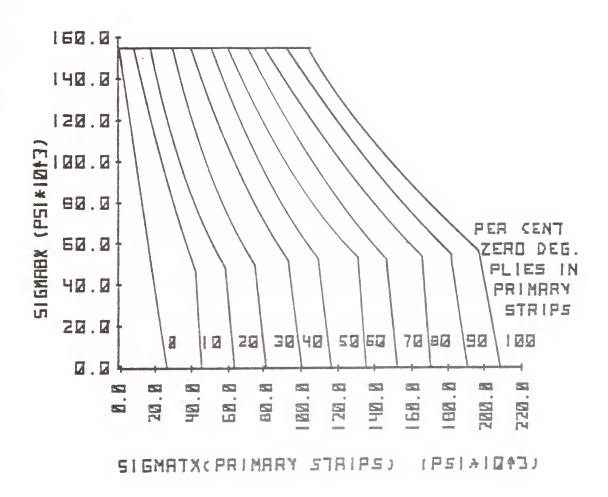


FIGURE 44. ULTIMATE STRESS INTERACTION CURVE FOR A

1.0 IN. LONG BUFFER STRIP PLATE MADE FROM NARMCO

5208/T300 [0/±45] MATERIAL WITH 0.833 IN. WIDE PRIMARY

STRIPS, A 1.0 IN. WIDE BUFFER STRIP, AND A 0.25 IN.

DIAMETER CENTRAL HOLE

VARIATION OF ULTIMATE BEARING STRESS
WITH BYPASS STRESS IN THE PRIMARY
STRIPS - BUFFER STRIP JOINT

HOLE DIRM. = 0.4375 IN.
BUFFER STRIP WIDTH = 4.00 DIRM.
PRIMARY STRIP WIDTH = 3.33 DIRM.

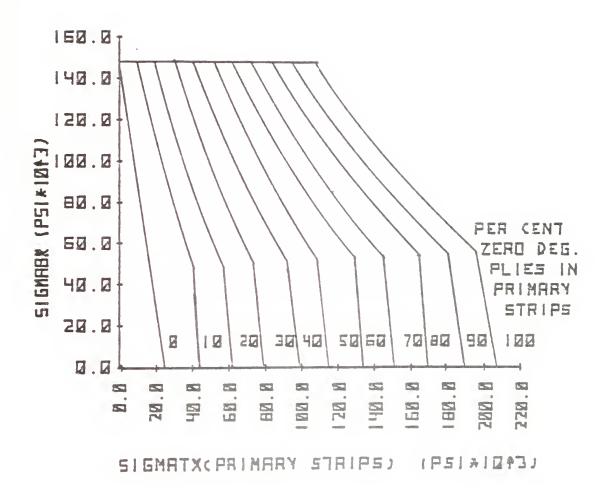
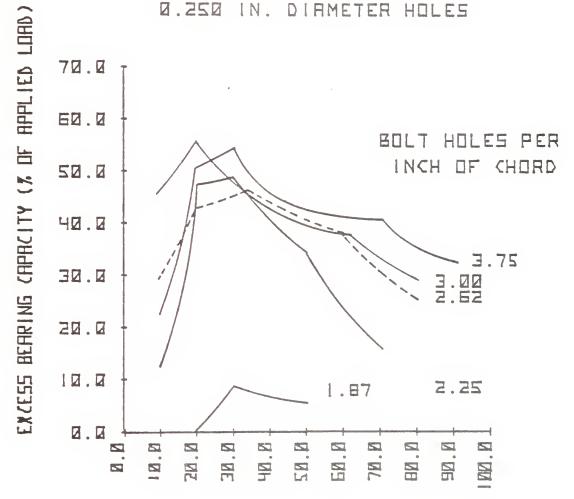


FIGURE 45. ULTIMATE STRESS INTERACTION CURVE FOR A 1.75 IN. LONG BUFFER STRIP PLATE MADE FROM NARMCO 5208/T300 [0/±45] MATERIAL WITH 1.46 IN. WIDE PRIMARY STRIPS, A 1.75 IN. WIDE BUFFER STRIP, AND A 0.4375 IN. DIAMETER CENTRAL HOLE

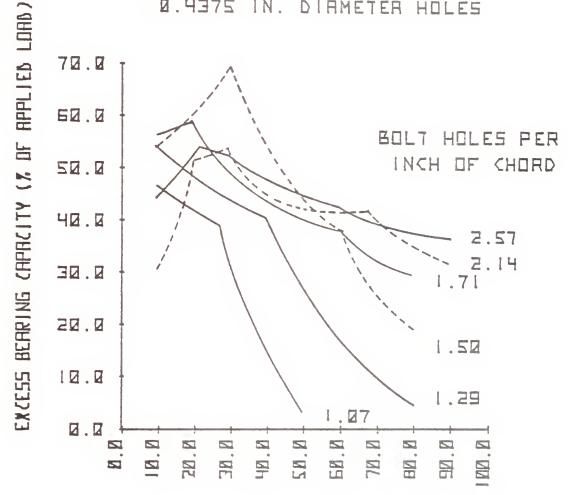
VARIATION OF EXCESS GERRING CAPACITY WITH LAMINATE COMPOSITION BUFFER STRIP JOINT 0.250 IN. DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

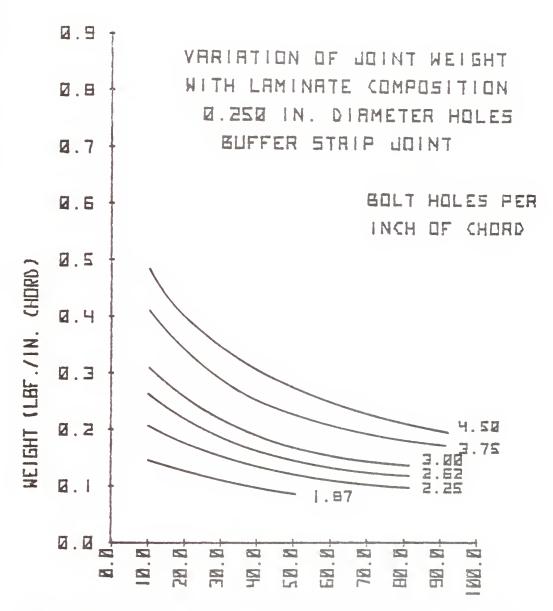
FIGURE 46. VARIATION OF EXCESS BEARING CAPACITY WITH LAMINATE COMPOSITION FOR BUFFER STRIP JOINTS WITH 0.25 IN. DIAMETER HOLES

VARIATION OF EXCESS BERRING CAPACITY
WITH LAMINATE COMPOSITION
BUFFER STRIP JOINT
D.4375 IN. DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT DUTBORAD HOLE

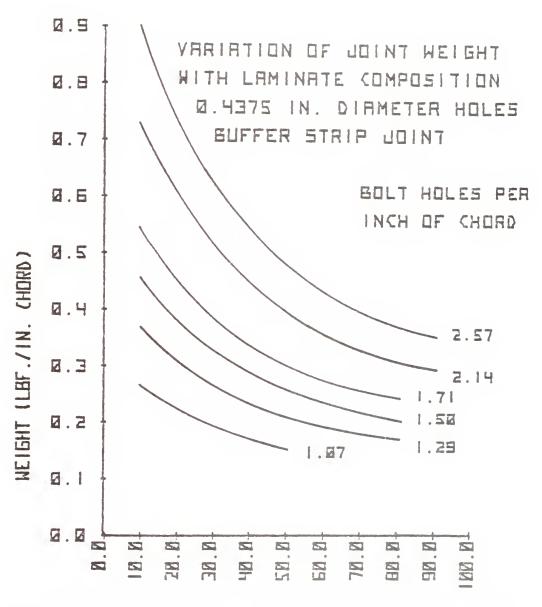
FIGURE 47. VARIATION OF EXCESS BEARING CAPACITY WITH LAMINATE COMPOSITION FOR BUFFER STRIP JOINTS WITH 0.4375 IN. DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

FIGURE 48. VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION FOR BUFFER STRIP JOINTS WITH 0.25 IN.

DIAMETER HOLES



PER CENT ZERO DEG. PLIES AT OUTBOARD HOLE

FIGURE 49. VARIATION OF JOINT WEIGHT WITH LAMINATE COMPOSITION FOR BUFFER STRIP JOINTS WITH 0.4375 IN. DIAMETER HOLES

TABLE I

SUMMARY OF DESIGN CONDITIONS AND ASSUMPTIONS

- 1. The joints are made from NARMCO 5208/T300 $\left[0/\pm45\right]$ graphite-epoxy laminated material.
- 2. Skin thickness varies linearly within a joint.
- 3. All bolt holes in a joint are of the same diameter.
- 4. The interbolt strain level is 3000 micro-in./in.
- 5. In the theoretical developments for both buffer strip and non-buffer strip joints it was assumed that only tensile and shear loads were to be carried.
- 6. Each row of bolts reacts an equal portion of the applied tensile load.
- 7. The applied shear load is reacted by the inboard row of bolts.
- 8. The minimum number of rows of bolts in any joint is three.
- 9. Wing taper is disregarded.
- 10. The inboard row of bolts is in all ±45 degree laminate.
- 11. The maximum joint length is ten inches.
- 12. In the non-buffer strip joints, there is a four-holediameter spacing between adjacent rows of bolt hole centers.
- 13. In the non-buffer strip joint, the laminate between the inboard and next to inboard bolt holes must contain at least five per cent zero degree plies.
- 14. In the buffer strip joints, the buffer strip width is

- four hole diameters. The primary strips are each 3.335 hole diameters wide.
- 15. Weight and excess bearing capacity calculations were made for assumed load conditions N $_{\rm X}$ = 20,000 lbf./in. and N $_{\rm XY}$ = 0.

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FORMAT (7, 'SUM OF THE REACTIONS'; 7,7,3)

FORMAT (5X,2615,4)

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FORMAT (7, 'SUM OF THE EXTERNAL END OF THE EXTERNAL INTEGER*2 (1-N)

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DC 20 [=1,NLEL VRNO(I) WRITE (6,50) I.LYRNO(I) WRITE (6,51) J.LAMAT(I,J),TKLAM(I,J),ORLAM(I,J) DO 20 J.L J.LAMAT(I,J),TKLAM(I,J),ORLAM(I,J) REAC THE CONSISTENT LOAD VECTOR (IF REQUIRED) IF ((NTLO+NTBY+NTIN).EQ.O) RETURN READ (5,52) J.J.T.CLX,CLY,THNP(I) CLOAD(IJT,1) = CLOAD(IJT,2) + CLY CLOAD(IJT,2) = CLOAD(IJT,2) + CLY CLOAD(IJT,2) = CLOAD(IJT,2) + CLY CNTINUE (6,54) MJT,NJT STOP WRITE (6,54) MJT,NAT STOP WRITE (6,55) MMT,NMAT STOP WRITE (6,56) MJT,NCLOAD STOP WRITE (6,56) MJT,NCLOAD STOP WRITE (6,59) MLYR,L	FCRMAT (1048) FCRMAT (11048) FCRMAT (1015,5X,15) FCRMAT (1015,5X,15) FCRMAT (1015,5X,15) FCRMAT (1015,5X,15) FORMAT (1015,5X,15) FORMAT (1015,5X,15) FORMAT (1015,5X,15) FORMAT (1015,5X,15) FORMAT (1015,5X,15) FORMAT (1015,5X,15) FCRMAT (1015,5X,15) FCRMAT (1015,5X,16) FCRMAT (1015,5X,1
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MATN = NCON(IK;14)
CALL STFMAT (ELAST;
TK = ELCON(MATN;7)
N = NCON(IK;13) *8
THICKNESS = 1. FOF
IF (NSTRES.EQ.1) TH
CALL QUAD5 (STK; AK;
WRITE (10) SS;SN 50 NCON(IK,15 IC.NE.1) GO VC (IK) NCON (IX -11-2 1+K -1)+K II FL R0 R0 1,2 , NPE +0-1 , NPE NP (IK=1,NE *NPEL N- .1 1, *DW-÷ II II \sim 2 NN = 1 00 3 J1=1 ---11 |--H 11 HΣ※ II ∑ 0-35-11 ~ ~~ ---911-11 00 11 9 9 91111 9 H \bigcirc 002 00 \Box OSS ш S \circ \circ $\circ\circ$

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EXHIBITING TWO DIMENSIONAL CRIHOTROPY, FOR ANISOTROPIC MATERIALS,
THE ELEMENTS OF THIS MATRIX ARE FIRST COMPUTED IN THE MATERIALS
BASEL L-T COORDINATE SYSTEM AND THEN TRANSFURMED TO THE PROBLEM
BASED X-Y COORDINATE SYSTEM.
IMPLICIT REAL*8(A-H, O-Z)
IMPLICIT REAL*8(A-H, O-Z)
IMPLICIT REAL*8(A-H, O-Z)
IMPLICIT NTEGER*2(I-N)
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IMPLICIT INTEGER*2(I-N)
CIMENSION AJ(2,2), AJIN(2,3), AK(24,24)
CCMMCN COORD(12,2), ELAST(3,2ER) = 0.000
                     AK, X, Y, B, N)
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IES,NGP,LM(12),LJT(12),NTLD,NTBY,NTIN,NL
CCMMON /FLPL/ COARD(217,2),CLOAD(217,2)
I(182),THNP(217)
CCMMON COORD(12,2),ELAST(3,3),SS(36,24)
DIMENSION SSJNT(217,7), SNJNT(217,7),
DIMENSION TEEL(12)
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X; 'EPS Y'; 'S-T-R-E-S-S-E-S', 'S-T-R-A-S-E-S', 'S-T-R-A-S-S-E-S', 'S-T-R-A-S-S-E-S', 'S-T-R-B-S-S-E-S', 'S-T-R-B-S-S-IS'; 'S-IS'; 'S-IS'; 'S-IS'; 'S-IS'; 'S-T-R-E-S-S-S-IS'; 'S-IS'; 'S-IS'; 'S-T-R-E-S-S-S-IS'; 'S-IS'; 
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13; 7X; EPS Y; 7X; 6AMMA

20 FCRMAT (7,715,8612,4,5X,1)

21 FORMAT (7/7,1X; A-V-E-R-1

1 //5X; 191NT; A-V-E-R-A

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22 FCRMAT (7/7,1X; A-V-E-R-A

1 //5X; GAMMA ; S; MAX; 7X; S

22 FCRMAT (7/7,1X; A-V-E-R-A

1 //5X; GAMMA ; S; MAX; 7X; S

22 FCRMAT (7/7,1X; A-V-E-R-A

1 //5X; GAMMA ; S; MAX; 7X; S

22 FCRMAT (7/7,1X; A-V-E-R-A

1 //5X; GAMMA ; S; MAX; 7X; S

24 FCRMAT (7/7,1X; A-V-E-R-A

1 //5X; GAMMA ; S; MAX; TX; S

27 FCRMAT (7/7,1X; A-V-E-R-A

27 FCRMAT (7/7) S

28 FCRMAT (7/7) S

29 FCRMAT (7/7) S

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DC 9 J=2,NBAND

IROW = IEQ-J+1

ICOL = IEQ-1+J

IF (IROW.LT.1) GO TO 8

ALOAD(IROW) = ALOAD(IROW)-BGK(IROW,J)*DXY

IF (ICOL.GT.NEQ) GO TO 9

ALOAD(ICOL) = ALOAD(ICOL)-BGK(IEQ,J)*DXY

CCNTINUE
                                                                       D(IEQ)-BGK(IEQ,1)*DXY
                                                                                                                                                                                                      .LT.1) GO TO 14
(IROW,JM)*CAL+BGK(IROW,J)*SAL
(IROW,J)*CAL-BGK(IROW,JM)*SAL
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                  3),
                 14,6,10,11,1
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                                                                                                                          IF (IDIA-EQ.1) GO TO 1

GC TO 16

DXV = CLOAD(IJT,1)

GO TO 7

IDIA = 1

DXY = CLOAD(IJT,1)

GC TO 7

ALPHA = CLOAD(IJT,2)*P

CAL = DCOS(ALPHA)

SAL = ESIN(ALPHA)

IECP = IEQ+1
                               10
IJT = NBC(I; 1)

KCDE = 1JT*2-1

KCDE = NBC(I; 2)

ILIA = 0

GC TO (1,3,4,6,10,1)

IEQ = IEQ+1

BGK(IEQ; 1) = ABGN

IF (IDIA.EQ.1) GO TO

GC TO 16

GC TO 2

GC TO 2

IDIA = 0

GO TO 1

CXY = CLOAD(IJT, 2)

IEG = IEQ+1

ALOAD(IEQ) = ABGN
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BGK(IEQP, JM), *

IEQP, JM) = A3

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CMMON /MDIM/MEL

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CCMMON /INT/ NEL,NJT,NMAT,NCLOAD,NPBC,NCON(182,15),1

ES,NGP,LM(12),LJT(12),NLEL

COMMON /MDIM/ MEL,MJT,MMT,MBD,MLEL,MLYR

CCMMON /FLL/ COARD(217,2),TLOAD(217,2),ELCON(10,7)

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(CMMON /LOAD/ TEMP(12),BDFY(12,2),DSPN(12,2),TK,ALPI

1,NTIN,NCARD

CCMMON /LOAD/ TEMP(12),BDFY(12,2),DSPN(12,2),TK,ALPI

CCMMON /LOAD/ TEMP(12),BDFY(12,2),DSPN(12,2),TK,ALPI

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CCMMON /FLLAM/ TKLAM(50,100),ORLAM(50,100)

CCMMON /FLLAM/ TKLAM(50,100),ORLAM(50,100)

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FVEC(IE) +CLOAD(IJ;
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IF (INDIC.NE.O) GO TO 4

ALPHA = ELCON(IMAT;6)

IF (NN.NE.O) ALPHA = ALP

CCNTINUE

TK = ELCON(IMAT;7)

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LCODE = 3
CALL FLOAD (FVEC
WRITE (6,23) I,N
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= 2*L-1
= 10+1
NCON(1,L)
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NJT = NBC(II

NJT = NBC(IIII)

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10 = 2*J-1
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CLGAD(1J,1) =
CLGAD(1J,2) =
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IJ = LM
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DC 20 I=1,NJT
IF (NCARD.NE.0) WRITE (7,21) I,CLOAD(I,1),CLOAD(I,2),THNP(I)
WRITE (6,21) I,CLOAD(I,1),CLOAD(I,2),THNP(I)
CCNTINUE
LOAD(NJT,1)*COSA+CLOAD(NJT,2)*SINA
RO
SINA = DSIN(ALF)
CLCAD(NJT,1) = C(
CLCAD(NJT,2) = ZI
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DC 5 I=1,NJT
READ (5,30) IJT,COARD(IJT,1),COARD(IJT,2),CLOAD(IJT,1),CLOAD(IJT,2]
I),IND
IF (IND,EQ.0) GO TO 5
ALF = COARD(IJT,2)*PI/180.000
CCSA = DCOS(ALF)
SINA = DSIN(ALF)
XC = COARD(IJT,1)*COSA
YC = COARD(IJT,1)*SINA
COARD(IJT,1) = XC
CCARD(IJT,1) = XC
CCARD(IJT,1) = XC
CCARD(IJT,1) = XC
                                                                                                                              READ (5,27) NEL, NJT, NMAT, NCLOAD, NPBC, NSTRES, NGP, NTLD, NTBY, NTIN, NCA
IRE, NLEL
WRITE (6,28) NEL, NJT, NMAT, NCLOAD, NPBC, NSTRES, NGP, NTLD, NTBY, NTIN, NC
IARD, NLEL
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DC 2 I=1,MMT INDK(I) = 0
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                                             DO 3 I=1, MEL
ANGL(I) = ZF
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LYRNO(I)
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,37) IJT, (NCON(IJT, J), J=1,14), ANGL(IJT), NCON(IJT,15
                   I, COARD(I, 1), COARD(I, 2), CLOAD(I, 1), CLOAD(I, 2)
                                                                                                                                            I=1, NEL
(6,38) I, (NCON(I, J), J=1,14), ANGL(I), NCON(I,15
                                                DC 7 I=1,NMAT
READ (5,32) IMAT,INDK(IMAT),(ELCON(IMAT,J),J=1,7)
                                                                      IC 8 I=1,NMAT
IRITE (6,34) I,(ELCON(I,J),J=1,7),INDK(I)
CNTINUE
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5,40) (NBC(I,J),J=1,2)
(6,41) (NBC(I,J),J=1,2)
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NBC(NPBC,2)
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READ (5,43) ((LAMAT(LAMTP,J),TKLAM(LAMTP,J),ORLAM(LAMTP,J)),J=1,L WRITE (6,44) DO 20 I=1,NLEL WRITE (6,45) I.LYRNO(I)	LL = LYRNO(I) DO 20 J=1,LL WRITE (6,46) J,L	1 NLDC = N IF (NLDC READ CON	MKITE (0;4 00 22 I=1, 2 READ (5,48	DO 23 I=1,NJT 23 WRITE (6,49) I,THNP(I),BYNP(I,1),BYNP(I,2),DPIN(I,1),DPIN(I,2) RETURN 24 WRITE (6,50)	5 FORMAT (10A8) 6 FORMAT (1215) 7 FCRMAT (1215) 8 FORMAT (1215) 8 FORMAT (1215) 8 FORMAT (1.2.15) 8 FO
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END

SUBROUTINE STFMAT (MATN, THETA, INDIC, NSTRES)

SUBROUTINE ASSEMBLES THE ELASTIC STIFFNESS MATRIX FOR A HOOKEAN

C ELEMENT. THE SUBROUTINE CALCULATES AND STORES IN C(3x3) THE VALUES

C ELEMENTS OF THIS MATRIX FOR ISOTROPIC MATERIALS

C ETHER PLANE STRAIN OR PLANE STRESS ONF FOR ANISOTROPIC MATERIALS

C ETHER PLANE STRAIN OR PLANE STRESS ONF FOR ANISOTROPIC MATERIALS

C EXHIBITING TWO DIMENSIONAL ORTHOTROPY. FOR ANISOTROPIC MATERIALS

C EXHIBITING TWO DIMENSIONAL ORTHOTROPY. FOR ANISOTROPIC MATERIALS

C EXHIBITING TWO DIMENSIONAL SYSTEM AND THEN TRANSFORMED TO THE PROBLEM

C BASED L-T COORDINATE SYSTEM AND THEN TRANSFORMED TO THE PROBLEM

IMPLICIT REAL*8(A-H, 0) - Z)

C MADON /FL/ COARD(217, 2), TLOAD(217, 2), ELCON(10, 7), TITLE(10), THNP

1 (217), BYNP(217, 2), DPIN(217, 2), ANGL(182)

C CMMON /FL/ COARD(12, 2), C(3, 3)

DIMENSION A(3, 3)
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= THETA+ORLAM(LAMTP, I)

IC = INDK(MATN)

RES = NN

STFMAT (MATN, PHI, INDIC

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CGS3 = DCGS(THRAD) **3
CGS4 = DCGS(THRAD) **4
SIN1 = DSIN(THRAD) **4
SIN2 = DSIN(THRAD) **4
SIN3 = DSIN(THRAD) **4
TWG = DSIN(THRAD) **4
TWG = CSIN(THRAD) **4
TWG = 2.0D0
C(1,1) = 2.0D0
C(1,2) = A(1,1) *CGS4+TWG*(A(1,2)-TWG*A(3,3)) *SIN3*CGS1
C(1,3) = A(1,1) *SIN3*CGS1
C(2,3) = A(1,1) *SIN4+TWG*(A(1,1)-A(1,2)-TWG*A(3,3)) *SIN1*CGS3
C(2,3) = A(1,1) +A(2,2)-TWG*A(3,3)
C(2,3) = A(1,1) +A(2,2)-TWG*A(3,3)
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FVEC(II) = FVEC(II)+WVEC(II)*AIA(I,J)
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FVEC(II) = FVEC(II)+WVEC(II)*AIA(I,J)
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WVEC(II) = (BTD(II,1)+BTD(II,2))*CFT
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CFT+VAL(II)*TEMP(II)
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SHAPE (VAL, X, Y, NPEL)
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IO = 2*II-1
IE = IO+1
WVEC(IO) = VAL(I
        DO 9 JJ=1,3
BTD(II,JJ) =
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BTD(II,JJ)
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SUBRGUTINE SHAPE (VAL, X, Y, N PEL)
IMPLICIT REAL*8(A-H, 0-2)
IMPLICIT INTEGER*2(I-N)
DIMENSION VAL(12), XYL(4,2), XYQ(8,2), XYC(12,2), I
DATA XYL/1.0D0,-1.0D0,-1.0D0,1.0D0,1.0D0,1.0D0,1.0
DATA XYQ/1.0D0,0.0D0,-1.0D0,-1.0D0,-1.0D0,0.000,1.0
                                                                                                                                    BID(II, JJ)+B(KK, II)*ELAST(KK, JJ)
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SK(II,JJ) = SK(II,JJ)+BTD(II,KK)*B(KK,JJ)
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WVEC(II) = WVEC(II)+SK(II,JJ)*DSPC(JJ)
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FVEC(II) = FVEC(II)+WVEC(II)*AIA(I,J)
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WVEC(II) = -WVEC(II)*TK*DTJ
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WVEC(II) = 0.0D0
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